

# Implementation of Digital Optical Switches and Signal Routers for High-Speed Communication

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### Introduction

- Photonics has settled its effectiveness in various switching functions due to its key features of large bandwidth, EMI immunity, integrability and high speed.
- The use of light offers the possibility of high-speed operation around  $10^4$  times faster than that conceivable employing electronic circuits.
- Lightwaves of different frequencies (or wavelengths) can be used within the same guided wave channel or device.
- Linear electro-optic effect (Pockels Effect) can be efficiently used to obtain switching phenomena based on integrated MZIs.
- The integrated MZIs are used to design various WDM components such as combinational and sequential logic devices, signal routers, wavelength selectors etc.

### **Motivation of work**

- In the switching context of WDM components, integrated photonic devices have a distinct advantage of high speed and low signal degradation over their electronic counterparts in this area.
- To fulfill the growing demand of high speed communication, the WDM systems are acquiring popularity worldwide.
- Successful demonstrations and development have been seen on the component level (switches, routing devices), system level (large photonic switch architectures), and the network level (wavelength-switched networks).

### **Motivation cont....**

• Till date, several combinational and sequential circuits have been proposed utilizing various technologies such as periodically poled LiNbO<sub>3</sub> (PPLN), Erbium doped optical amplifier (EDFA) and Fabryperot laser diodes (FP-LDs).

<u>The following problem occurs in the previous work:</u>

- ✓ PPLN based logic circuits require numerous light sources and so, they are costly.
- ✓ Erbium doped fiber amplifier operates exclusively at low speeds upto 1 Gbps.

Devices implemented with FP-LDs are complex in the sense that more number of FP- LDs and some external devices are required to implement even a simple logic circuit.
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#### **Motivation cont....**

✓ SOAs based logic circuits need interferometric structure that requires numerous devices with matching characteristics and proper control.

Electro-optic modulator (EOM) seems to be an interesting substitute because of its distinct features of being:

- ✓ lightweight,
- ✓ miniature,
- ✓ immune to electromagnetic interference,
- ✓ wider bandwidth (faster switching times),
- ✓ lower drive power,
- $\checkmark$  and inherently compatible with optical fiber.

#### **Motivation cont....**

• LiNbO<sub>3</sub> possess a combination of unique electro-optical, acoustic, piezoelectric, and non-linear optical properties making it a suitable material for implementation of integrated photonic devices.

• Beam propagation method (BPM) is one of the popular numerical methods. The mathematical details of the mode concept satisfying mode solution are reviewed.



Figure: General block diagram of Wavelength Division Multiplexed System

- ➤ Wavelength-division multiplexing (WDM) is a technology which multiplexes a number of optical carrier signals onto a single optical fiber by using different wavelengths.
- Some of the optical WDM network components are: multiplexers (MUX), demultiplexers (De-MUX), Single mode DFB laser, power divider, power splitters, Optical adductrop multiplexers (OADM), WDM Couplers etc.

#### **Pockels Effect**



(b) Applied field along y in  $LiNbO_3$  modifies the indicatrix and changes  $n_1$  and  $n_2$  change to  $n'_1$  and  $n'_2$ .

(3)

(4)

$$n'_{1} \approx n_{1} + \frac{1}{2}n_{1}^{3}rE_{a}$$
 and  $n'_{2} \approx n_{2} - \frac{1}{2}n_{1}^{3}rE_{a}$  (1)  
 $\varphi_{1} = \frac{2\pi n'_{1}}{\lambda}L = \frac{2\pi L}{\lambda} \left(n_{0} + \frac{1}{2}n_{0}^{3}r\frac{V}{d}\right)$  (2)

$$\varphi_2 = rac{2\pi n_1'}{\lambda} L = rac{2\pi L}{\lambda} \Big( n_0 - rac{1}{2} n_0^3 r rac{V}{d} \Big)$$

$$\Delta \varphi = \varphi_1 - \varphi_2 = \frac{2\pi}{\lambda} n_0^3 r \frac{L}{d} V$$

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where,

 $\lambda \rightarrow Wavelength of the signal.$ 

$$n_0 \rightarrow Refractive index of the material.$$

 $d \rightarrow$  Separation between the electrodes.

$$r \rightarrow Electro - optic coefficients (m/V).$$

- $V \rightarrow Voltage applied across the waveguide.$ 
  - $L \rightarrow$  Length of the waveguide.



## Interferometric Modulator

Table: Different parameters to obtain particular voltage  $V\pi$ 

	•			
Parameters	Value of Parameters			
Wavelengths $(\lambda)$	1.33 μm			
Separation	6 µm			
between the				
electrodes (d)				
Refractive index	1.47			
Electro-optic	$36.6 \times 10^{-12} m/V$			
coefficients				
Substantial Length	10000 μm			
(L)				
$V_{\pi} = \frac{\lambda}{n^3} \frac{1}{r} \frac{d}{L} = 6.75 V$				



$$\begin{bmatrix} A \\ B \end{bmatrix} = \begin{bmatrix} \sqrt{1 - \alpha_1} & j\sqrt{\alpha_1} \\ j\sqrt{\alpha_1} & \sqrt{1 - \alpha_1} \end{bmatrix} \begin{bmatrix} E_{in} \\ 0 \end{bmatrix}$$
(5)
$$\begin{bmatrix} C \\ D \end{bmatrix} = \begin{bmatrix} e^{-j\varphi_1} & 0 \\ 0 & e^{-j\varphi_2} \end{bmatrix} \begin{bmatrix} A \\ B \end{bmatrix}$$
(6)

$$\begin{bmatrix} OUT_1\\ OUT_2 \end{bmatrix} = \begin{bmatrix} \sqrt{1-\alpha_2} & j\sqrt{\alpha_2}\\ j\sqrt{\alpha_2} & \sqrt{1-\alpha_2} \end{bmatrix} \begin{bmatrix} C\\ D \end{bmatrix}$$
(7)

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Figure: Schematic view of Mach Zehnder interferometer

Where,  $\alpha_1$  and  $\alpha_2 \rightarrow$ 

Attenuation constant of first and second directional coupler

 $\phi_1 and \, \phi_2 \, \rightarrow \, Phase \, arises \, \, due \, to \, application \, of \, voltage$ 

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Figure: Simulation of MZI due to the variation of the control signal *X*.

$$P_{out 1} = \left| \frac{OUT_1}{E_{in}} \right|^2 = \left| je^{-j(\varphi_0)} sin\left(\frac{\Delta\varphi}{2}\right) \right|^2 = sin^2\left(\frac{\Delta\varphi}{2}\right)$$
(8)  
$$P_{out 2} = \left| \frac{OUT_2}{E_{in}} \right|^2 = \left| je^{-j(\varphi_0)} cos\left(\frac{\Delta\varphi}{2}\right) \right|^2 = cos^2\left(\frac{\Delta\varphi}{2}\right)$$
(9)  
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# Design of NOT gate using MZI

Santosh Kumar et. al., Optical Engineering (SPIE), Vol. 52, No. 9, PP. 097106 (Sep. 20, 2013)

### Design of NOT gate using MZI



Figure: Design of NOT gate using Mach-Zehnder Interferometers.

$$\left|\frac{\text{OUT2}}{\text{E}_{\text{in}}}\right|^2 = \cos^2\left(\frac{\Delta\phi}{2}\right)$$

For calculation, it has been assumed that,

$$\phi_0 = \frac{\phi_1 + \phi_2}{2}$$
 and  $\Delta \phi = \phi_1 - \phi_2 = \frac{\pi}{V_{\pi}}X$ 

 $\phi_1$  and  $\phi_2$  are the phase angle generated at the upper arm and the lower arm of MZI respectively. Dr. Santosh Kumar

### Contd...

Table: Optical signal at the two ports due to different combination of control signal.

Control signals	Signal output at different ports			
Х	Port 1	Port 2 ( $\overline{X}$ )		
0	0	1		
1	1	0		



Figure: Simulation result of the NOT logic gate operation at different

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combination of the control signals.

# Design of AND Gate using MZIs

Santosh Kumar et. al., Proc. SPIE 9131, Optical Modelling and Design III, SPIE Photonics Europe 2014,

Brussels, **Belgium**, PP. 913120 (May 1, 2014).

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#### AND Gate



#### Matlab result of AND Gate

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$$\left|\frac{\text{OUT1}_{\text{MZI2}}}{\text{E}_{\text{in}}}\right|^2 = \sin^2\left(\frac{\Delta\phi_{\text{MZI1}}}{2}\right)\sin^2\left(\frac{\Delta\phi_{\text{MZI2}}}{2}\right)$$

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#### BPM result of AND Gate



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# Design of OR gate using MZIs

Santosh Kumar et. al., Journal of Optical Communications (Degruyter), Dec. 2016.



Output port 2 (OR Logic Gate) =  $m_1 + m_2 + m_3$ 



#### BPM result of OR Gate



# Design of Universal Logic Gates using MZIs

Santosh Kumar et. al., Applied Optics (OSA), Vol. 54, Issue 28, pp. 8479-8484 (Sept. 30, 2015).

#### Design of universal logic gates



Figure: Schematic diagram of NOR gate using the MZIs.



Figure: Schematic diagram of NAND gate using the MZIs.

Table: Optical signal at the different ports due to different combination of control signals.

Contro	ol signals	Signal ou	tput at different p	orts
X	Y	Port 1	Port 2 (X NOR Y)	Port3
0	0	0	1	0
0	1	0	0	1
1	0	1	0	0
1	1 <del>Dr. Santo</del>	1 <del>sh Kumar-</del>	0	0

Table: Optical signal at the different ports due to different combination of control signals.

Control signals		Signal output at different ports			
X	Y	Port 1	Port 2 (X NAND Y)	Port 3	
0	0	0	1	1	
0	1	0	1	0	
1	0	1	1	0	
1	1	1	0	0	



Figure: MATLAB simulation result of the NOR gate.

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Figure: MATLAB simulation result of the NAND gate.

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Figure: Results of NOR logic operation for different combination of control signals (X and Y) obtained through Beam propagation method.



Figure: Results of NAND logic operation for different combination of control signals (X and Y) obtained through Beam propagation method.

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# Design of XOR/XNOR Gates using MZIs

Santosh Kumar et. al., Optik (Elsevier), Vol. 125, pp. 5764 - 5767 (August 27, 2014).

#### **XOR/XNOR Gates**



Output port 2 (XOR Logic Gate) =  $m_1 + m_2$ 

$$=\cos^{2}\left(\frac{\Delta\phi_{\rm MZI1}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{\rm MZI2}}{2}\right)+\sin^{2}\left(\frac{\Delta\phi_{\rm MZI1}}{2}\right)\cos^{2}\left(\frac{\Delta\phi_{\rm MZI2}}{2}\right)$$

Output port 1 (XNOR Logic Gate) =  $m_3 + m_4$ 

$$= \cos^{2}\left(\frac{\Delta\phi_{MZI1}}{2}\right)\cos^{2}\left(\frac{\Delta\phi_{MZI2}}{2}\right) + \sin^{2}\left(\frac{\Delta\phi_{MZI1}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI2}}{2}\right)$$
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### BPM layout and Results



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# Design of Full-Adder/Subtractor using the MZIs

Santosh Kumar et. al., Optics Communication (Elsevier), Vol. 324, PP. 93-107 (August 15,

2014).

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## Design of Full-Adder/Subtractor using the MZIs



## Mathematical Expressions:

$$\begin{split} D_{7} &= \left| \frac{OUT1_{MZI4}}{E_{in}} \right|^{2} = \sin^{2} \left( \frac{\Delta \phi_{MZI1}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{MZI2}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{MZI4}}{2} \right) \\ D_{6} &= \left| \frac{OUT2_{MZI4}}{E_{in}} \right|^{2} = \sin^{2} \left( \frac{\Delta \phi_{MZI1}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{MZI2}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{MZI4}}{2} \right) \\ D_{5} &= \left| \frac{OUT1_{MZI5}}{E_{in}} \right|^{2} = \sin^{2} \left( \frac{\Delta \phi_{MZI1}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{MZI2}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{MZI5}}{2} \right) \\ D_{4} &= \left| \frac{OUT2_{MZI5}}{E_{in}} \right|^{2} = \sin^{2} \left( \frac{\Delta \phi_{MZI1}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{MZI2}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{MZI5}}{2} \right) \\ D_{3} &= \left| \frac{OUT1_{MZI6}}{E_{in}} \right|^{2} = \cos^{2} \left( \frac{\Delta \phi_{MZI1}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{MZI3}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{MZI6}}{2} \right) \\ D_{2} &= \left| \frac{OUT2_{MZI6}}{E_{in}} \right|^{2} = \cos^{2} \left( \frac{\Delta \phi_{MZI1}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{MZI3}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{MZI6}}{2} \right) \\ D_{1} &= \left| \frac{OUT1_{MZI7}}{E_{in}} \right|^{2} = \cos^{2} \left( \frac{\Delta \phi_{MZI1}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{MZI3}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{MZI7}}{2} \right) \\ D_{0} &= \left| \frac{OUT1_{MZI7}}{E_{in}} \right|^{2} = \cos^{2} \left( \frac{\Delta \phi_{MZI1}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{MZI3}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{MZI7}}{2} \right) \\ \end{split}$$

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### BPM Results of Full Adder



## BPM Layout of Full Subtractor



DIFFERENCE

$$= \cos^{2}\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\cos^{2}\left(\frac{\Delta\varphi_{MZI3}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI7}}{2}\right) + \cos^{2}\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI3}}{2}\right)\cos^{2}\left(\frac{\Delta\varphi_{MZI6}}{2}\right) + \sin^{2}\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI2}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI4}}{$$

$$\begin{aligned} &= \cos^{2}\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\cos^{2}\left(\frac{\Delta\varphi_{MZI3}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI7}}{2}\right) + \cos^{2}\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI3}}{2}\right)\cos^{2}\left(\frac{\Delta\varphi_{MZI6}}{2}\right) \\ &+ \cos^{2}\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI3}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI6}}{2}\right) + \sin^{2}\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI2}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI4}}{2}\right) \end{aligned}$$

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## BPM Results of Full Subtractor



# Design of an optical N-bit reversible ripple carry adder

Santosh Kumar et. al., IEEE Workshop on Recent Advances in Photonics, Indian Institute of Science, Bangalore, 2015.

# Design of an optical N-bit reversible ripple carry adder



Fig. 23: Schematic diagram of optical reversible gate-I (ORG-I).

S. No.	Control signal 'A' (V)	Control signal 'B' (V)	Control signal 'C' (V)	$AB + (A \oplus B)C$	$(A \oplus B)$	$A\overline{B} + (\overline{A \oplus B})C$
1	0	0	0	0	0	0
2	0	0	6.75	0	0	1
3	0	6.75	0	0	1	0
4	0	6.75	6.75	1	1	0
5	6.75	0	0	0	1	1
6	6.75	0	6.75	1	1	1
7	6.75	6.75	0	1	0	0
8	6.75	6.75	6.75	1	0	1

Table 6: State table for optical reversible gate-I (ORG-I)



Fig. 24: Schematic diagram of optical reversible gate-I (ORG-I).

S. No.	Control signal 'A' (V)	Control signal 'B' (V)	Control signal 'C' (V)	$X = A\overline{B} + BC$	$Y = \overline{B}C + \overline{A}B$	$Z = AB + \overline{B}C$
1	0	0	0	0	0	0
2	0	0	6.75	0	1	1
3	0	6.75	0	0	1	0
4	0	6.75	6.75	1	1	0
5	6.75	0	0	1	0	0
6	6.75	0	6.75	1	1	1
7	6.75	6.75	0	0	0	1
8	6.75	6.75	6.75	1	0	1

Table 7: State table for optical reversible gate-II (ORG-II)



Figure: Schematic diagram of an n-bit reversible ripple carry adder using ORG-I and ORG-II.

Sum, 's' and carry  $C_j$  are given as

$$s_{j} = \begin{cases} a_{j} \bigoplus b_{j} \bigoplus c_{j} & for \quad 0 \le j \le n-1 \\ C_{n} & for \quad j=n \end{cases}$$
$$c_{j} = \begin{cases} C_{0} & ; \quad j=0 \\ a_{j-1}b_{j-1} + (a_{j-1} \bigoplus b_{j-1})C_{j-1} & ; \quad 1 \le j \le n \end{cases}$$



Figure OptiBPM layout for optical reversible gate-I (ORG-I).



Figure: OptiBPM simulation results for ORG-I, when control signals A, B and C are varied from 000 to 011.

Figure: OptiBPM simulation results for ORG-I, when control signals A, B and C are varied from 100 to 111.



Fig.: OptiBPM layout for optical reversible gate-II (ORG-II).



Fig.: OptiBPM simulation results for ORG-II, when control signals A, B and C are varied from 000 to 011. Dr. Santosh Kumar

Fig.: OptiBPM simulation results for ORG-II, when control signals A, B and C are varied from 100 to 111.

# Design of 2-bit Multiplier using MZIs

Santosh Kumar et. al., Optical and Quantum Electronics (Springer), Vol. 47, Issue 12, pp 3667-

3688 (August 20, 2015).

# Design of 2-bit Multiplier using MZIs



# Mathematical expression of 2-bit Multiplier

The normalized output power at different output ports can be represented by the following equations;

At Port  $M_0$ ;

$$M_0 = \left| \frac{OUT1_{MZI3}}{E_{in}} \right|^2 = \left\{ \sin^2 \left( \frac{\Delta \phi_{MZI1}}{2} \right) \sin^2 \left( \frac{\Delta \phi_{MZI3}}{2} \right) \right\}$$

At Port  $M_1$ ;

$$M_{1} = \left\{ \sin^{2} \left( \frac{\Delta \phi_{MZI9}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{MZI10}}{2} \right) \right\} + \left\{ \cos^{2} \left( \frac{\Delta \phi_{MZI9}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{MZI11}}{2} \right) \right\}$$

At Port  $M_2$ ;

$$M_{2} = \left\{ \sin^{2} \left( \frac{\Delta \phi_{MZI12}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{MZI13}}{2} \right) \right\} + \left\{ \cos^{2} \left( \frac{\Delta \phi_{MZI12}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{MZI14}}{2} \right) \right\}$$

At Port  $M_3$ ;

$$M_{3} = \left|\frac{OUT1_{MZI3}}{E_{in}}\right|^{2} = \left\{\sin^{2}\left(\frac{\Delta\phi_{MZI12}}{2}\right) \sin^{2}\left(\frac{\Delta\phi_{MZI13}}{2}\right)\right\}$$

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#### MATLAB Result of 2-bit Multiplier



Figure: MATLAB simulation results of 2-bit multiplier, when the magnitude of B is 0 and magnitude

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of A changes from 0 to 3.



Figure: MATLAB simulation results of 2-bit multiplier, when magnitude of B is 1 and magnitude of A changes

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from 0 to 3.



Figure: MATLAB simulation results of 2-bit multiplier, when magnitude of B is 2 and magnitude of A changes

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from 0 to 3.



Figure: MATLAB simulation results of 2-bit multiplier, when the magnitude of B is 3 and magnitude of A changes from 0 to 3.

### **BPM** Result of 2-bit Multiplier



0 and magnitudes A changes from 0 to 3.

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1 and magnitudes A changes from 0 to 3.



Figure: The results of 2-bit multiplier operation, when magnitude of B is 2 and magnitudes A changes from 0 to 3.

Figure: The results of 2–bit multiplier operation, when magnitude of B is 3 and magnitudes A changes from 0 to 3.

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# Design of 1-bit and 2-bit magnitude comparators

Santosh Kumar et. al., Optics Communications (Elsevier), Vol. 357, PP. 127-147 (Sept. 09, 2015).

# Design of 1-bit and 2-bit magnitude comparators



Figure: Schematic diagram of 1-bit comparator using the MZIs.



Dr. Santosh Kumar Figure: Schematic diagram of 2-bit comparator using the MZIs.

For case 1 (A = B);

$$OUT1 = \left|\frac{OUT1_{MZI2}}{E_{in}}\right|^{2} = \left\{\cos^{2}\left(\frac{\Delta\phi_{MZI1}}{2}\right)\cos^{2}\left(\frac{\Delta\phi_{MZI2}}{2}\right)\right\} + \left\{\sin^{2}\left(\frac{\Delta\phi_{MZI1}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI2}}{2}\right)\right\}$$

For case 2 (A < B);

$$OUT2 = \left|\frac{OUT1_{MZI3}}{E_{in}}\right|^2 = \cos^2\left(\frac{\Delta\varphi_{MZI1}}{2}\right) \sin^2\left(\frac{\Delta\varphi_{MZI2}}{2}\right) \sin^2\left(\frac{\Delta\varphi_{MZI3}}{2}\right)$$

For case 3 (A > B);



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Figure: Simulation result of 1-bit magnitude comparator.

For Case 1 (A = B):

$$\begin{aligned} \text{OUT1} &= \left| \frac{\text{OUT1}_{\text{MZ112}}}{\text{E}_{\text{in}}} \right|^2 \\ &= \left\{ \cos^2 \left( \frac{\Delta \phi_{\text{MZ11}}}{2} \right) \cos^2 \left( \frac{\Delta \phi_{\text{MZ12}}}{2} \right) \ \cos^2 \left( \frac{\Delta \phi_{\text{MZ16}}}{2} \right) \cos^2 \left( \frac{\Delta \phi_{\text{MZ19}}}{2} \right) \right\} + \left\{ \ \cos^2 \left( \frac{\Delta \phi_{\text{MZ19}}}{2} \right) \sin^2 \left( \frac{\Delta \phi_{\text{MZ12}}}{2} \right) \ \sin^2 \left( \frac{\Delta \phi_{\text{MZ12}}}{2} \right) \sin^2 \left( \frac{\Delta \phi_{\text{MZ12}}}{2} \right) \right\} \\ &+ \left\{ \ \cos^2 \left( \frac{\Delta \phi_{\text{MZ11}}}{2} \right) \ \cos^2 \left( \frac{\Delta \phi_{\text{MZ12}}}{2} \right) \ \sin^2 \left( \frac{\Delta \phi_{\text{MZ12}}}{2} \right) \ \sin^2 \left( \frac{\Delta \phi_{\text{MZ12}}}{2} \right) \right\} \\ &+ \left\{ \ \sin^2 \left( \frac{\Delta \phi_{\text{MZ16}}}{2} \right) \ \sin^2 \left( \frac{\Delta \phi_{\text{MZ12}}}{2} \right) \ \sin^2 \left( \frac{\Delta \phi_{\text{MZ12}}}{2} \right) \ \sin^2 \left( \frac{\Delta \phi_{\text{MZ12}}}{2} \right) \right\} \end{aligned}$$

For Case 2 (A < B):

$$\begin{aligned} \text{OUT2} &= \left| \frac{\text{OUT2}_{\text{MZI10}}}{E_{in}} \right|^2 \\ &= \sin^2 \left( \frac{\Delta \phi_{\text{MZI1}}}{2} \right) \quad \cos^2 \left( \frac{\Delta \phi_{\text{MZI2}}}{2} \right) \quad \cos^2 \left( \frac{\Delta \phi_{\text{MZI3}}}{2} \right) \quad \cos^2 \left( \frac{\Delta \phi_{\text{MZIB}}}{2} \right) + \quad \sin^2 \left( \frac{\Delta \phi_{\text{MZI6}}}{2} \right) \quad \cos^2 \left( \frac{\Delta \phi_{\text{MZI9}}}{2} \right) \\ &+ \quad \sin^2 \left( \frac{\Delta \phi_{\text{MZI1}}}{2} \right) \quad \sin^2 \left( \frac{\Delta \phi_{\text{MZI5}}}{2} \right) \quad \cos^2 \left( \frac{\Delta \phi_{\text{MZI2}}}{2} \right) \quad \cos^2 \left( \frac{\Delta \phi_{\text{MZI3}}}{2} \right) \\ &+ \quad \sin^2 \left( \frac{\Delta \phi_{\text{MZI1}}}{2} \right) \quad \cos^2 \left( \frac{\Delta \phi_{\text{MZI2}}}{2} \right) \quad \cos^2 \left( \frac{\Delta \phi_{\text{MZI3}}}{2} \right) \end{aligned}$$

For Case 3 (A > B):

$$\begin{aligned} \text{OUT3} &= \left|\frac{\text{OUT1}_{\text{MZ17}}}{\text{E}_{\text{in}}}\right|^2 \\ &= \sin^2\left(\frac{\Delta\phi_{\text{MZ12}}}{2}\right) \quad \sin^2\left(\frac{\Delta\phi_{\text{MZ13}}}{2}\right) \quad \cos^2\left(\frac{\Delta\phi_{\text{MZ11}}}{2}\right) \quad \cos^2\left(\frac{\Delta\phi_{\text{MZ4}}}{2}\right) + \quad \sin^2\left(\frac{\Delta\phi_{\text{MZ19}}}{2}\right) \quad \sin^2\left(\frac{\Delta\phi_{\text{MZ10}}}{2}\right) \quad \cos^2\left(\frac{\Delta\phi_{\text{MZ16}}}{2}\right) \\ &+ \quad \sin^2\left(\frac{\Delta\phi_{\text{MZ12}}}{2}\right) \quad \sin^2\left(\frac{\Delta\phi_{\text{MZ13}}}{2}\right) \quad \cos^2\left(\frac{\Delta\phi_{\text{MZ11}}}{2}\right) \quad \cos^2\left(\frac{\Delta\phi_{\text{MZ14}}}{2}\right) \\ &+ \quad \sin^2\left(\frac{\Delta\phi_{\text{MZ12}}}{2}\right) \quad \sin^2\left(\frac{\Delta\phi_{\text{MZ13}}}{2}\right) \quad \cos^2\left(\frac{\Delta\phi_{\text{MZ11}}}{2}\right) \quad \sin^2\left(\frac{\Delta\phi_{\text{MZ17}}}{2}\right) \end{aligned}$$



Figure: Simulation result of 1-bit magnitude comparator.

# Design of 1-bit and 2-bit magnitude comparators



Figure: Layout of 1-bit comparator using the MZIs.









to 3.

# Design of Parity Generator and Checker Circuit

#### Santosh Kumar et. al., Optics Communications (Elsevier), Vol. 364, PP. 195–224 (Dec.

07, 2015).

### Even Parity Generator



Figure: (a) Digital circuit and K-map of even parity generator. (b) Schematic diagram of even parity generator using MZIs Dr. Santosh Kumar

# Mathematical Expression for Even Parity

For Even Parity:  

$$p = \left[ sin^{2} \left( \frac{\Delta \phi_{1}}{2} \right) cos^{2} \left( \frac{\Delta \phi_{2}}{2} \right) + cos^{2} \left( \frac{\Delta \phi_{1}}{2} \right) sin^{2} \left( \frac{\Delta \phi_{2}}{2} \right) \right] \\
+ \left[ sin^{2} \left( \frac{\Delta \phi_{3}}{2} \right) cos^{2} \left( \frac{\Delta \phi_{4}}{2} \right) + cos^{2} \left( \frac{\Delta \phi_{3}}{2} \right) sin^{2} \left( \frac{\Delta \phi_{4}}{2} \right) \right] \\
+ \left[ sin^{2} \left( \frac{\Delta \phi_{5}}{2} \right) cos^{2} \left( \frac{\Delta \phi_{6}}{2} \right) + cos^{2} \left( \frac{\Delta \phi_{5}}{2} \right) sin^{2} \left( \frac{\Delta \phi_{6}}{2} \right) \right]$$

### MATLAB Results (Even Parity Generator)



Figure: MATLAB simulation result of Even Parity generator where B3 B2 B1 B0 varies from 0000 to 1111

## BPM Layout of Even Parity Generator



Figure: BPM layout of even parity generator.

### Simulation Result from BPM (Even Parity Generator)



Figure: BPM result to even parity generator where  $b_0 b_1 b_2 b_3$  varies from 0000 to1111.

Dr. Santosh Kumar

### Odd Parity Generator





 $p=(b_0\oplus b_1) \odot (b_2\oplus b_3)$ 



# Mathematical Expression for Odd Parity Generator

For Odd Parity:  

$$p = \left[ sin^{2} \left( \frac{\Delta \phi_{1}}{2} \right) cos^{2} \left( \frac{\Delta \phi_{2}}{2} \right) + cos^{2} \left( \frac{\Delta \phi_{1}}{2} \right) sin^{2} \left( \frac{\Delta \phi_{2}}{2} \right) \right] \\
+ \left[ sin^{2} \left( \frac{\Delta \phi_{3}}{2} \right) cos^{2} \left( \frac{\Delta \phi_{4}}{2} \right) + cos^{2} \left( \frac{\Delta \phi_{3}}{2} \right) sin^{2} \left( \frac{\Delta \phi_{4}}{2} \right) \right] \\
+ \left[ sin^{2} \left( \frac{\Delta \phi_{5}}{2} \right) sin^{2} \left( \frac{\Delta \phi_{6}}{2} \right) + cos^{2} \left( \frac{\Delta \phi_{5}}{2} \right) cos^{2} \left( \frac{\Delta \phi_{6}}{2} \right) \right]$$

## MATLAB Results (Odd Parity Generator)



Figure: MATLAB simulation result of odd Parity generator where  $B_3 B_2 B_1 B_0$  varies from 0000 to 1111

### BPM Layout of Odd Parity Generator



Figure: BPM layout of odd parity generator.

## Simulation Result from BPM (Odd Parity Generator)



Figure: BPM result to even parity generator where  $b_0 b_1 b_2 b_3$  varies from 0000 to1111.

## Even Parity Checker





 $\mathbf{PE} = (\mathbf{b}_0 \oplus \mathbf{b}_1 \oplus \mathbf{b}_2 \oplus \mathbf{b}_3 \oplus \mathbf{P})$ 

 $b_0 = 1$ 

Â

 $\mathbf{1}$ 

<1



Mathematical Expression for Even Parity Checker

For Even Parity:  

$$p = \left[ \sin^{2} \left( \frac{\Delta \phi_{1}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{2}}{2} \right) + \cos^{2} \left( \frac{\Delta \phi_{1}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{2}}{2} \right) \right] \\
+ \left[ \sin^{2} \left( \frac{\Delta \phi_{3}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{4}}{2} \right) + \cos^{2} \left( \frac{\Delta \phi_{3}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{4}}{2} \right) \right] \\
+ \left[ \sin^{2} \left( \frac{\Delta \phi_{5}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{6}}{2} \right) + \cos^{2} \left( \frac{\Delta \phi_{5}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{6}}{2} \right) \right] \\
+ \left[ \sin^{2} \left( \frac{\Delta \phi_{7}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{8}}{2} \right) + \cos^{2} \left( \frac{\Delta \phi_{7}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{8}}{2} \right) \right]$$
#### MATLAB Results (Even Parity Checker)



Figure: MATLAB simulation result of Even Parity Checker where  $B_3 B_2 B_1 B_0$  P varies from 00000 to 01111 Dr. Santosh Kumar

#### Contd..



Figure: MATLAB simulation result of Even Parity Checker where B<sub>3</sub> B<sub>2</sub> B<sub>1</sub> B<sub>0</sub> P varies from 10000 to 11111

#### BPM Layout of Even Parity Checker



Figure: BPM layout of even parity checker.

#### Simulation Result from BPM (Even Parity Checker)



#### Odd Parity Checker







 $\mathbf{PE} = (\mathbf{b_0} \oplus \mathbf{b_1}) \textcircled{\mathbf{0}} (\mathbf{b_2} \oplus \mathbf{b_3} \oplus \mathbf{P})$ 



Figure: (a) Digital circuit and K-map of odd parity checker (b) Schematic diagram of odd parity checker using **MZIs** Dr. Santosh Kumar

#### Mathematical Expression for Odd parity Checker

For Odd Parity:  

$$p = \left[ \sin^{2} \left( \frac{\Delta \phi_{1}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{2}}{2} \right) + \cos^{2} \left( \frac{\Delta \phi_{1}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{2}}{2} \right) \right] \\
+ \left[ \sin^{2} \left( \frac{\Delta \phi_{3}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{4}}{2} \right) + \cos^{2} \left( \frac{\Delta \phi_{3}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{4}}{2} \right) \right] \\
+ \left[ \sin^{2} \left( \frac{\Delta \phi_{5}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{6}}{2} \right) + \cos^{2} \left( \frac{\Delta \phi_{5}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{6}}{2} \right) \right] \\
+ \left[ \sin^{2} \left( \frac{\Delta \phi_{7}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{8}}{2} \right) + \cos^{2} \left( \frac{\Delta \phi_{7}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{8}}{2} \right) \right]$$

#### MATLAB Results (Odd Parity Checker)



Figure: MATLAB simulation result of Odd Parity Checker where B<sub>3</sub> B<sub>2</sub> B<sub>1</sub> B<sub>0</sub> P varies from 00000 to 01111 Dr. Santosh Kumar

#### Contd..



Figure: MATLAB simulation result of Odd Parity Checker where B<sub>3</sub> B<sub>2</sub> B<sub>1</sub> B<sub>0</sub> P varies from 10000 to 11111 Dr. Santosh Kumar

#### BPM Layout of Odd Parity Checker



Figure: BPM layout of odd parity checker.

#### Simulation Result from BPM (Odd Parity Checker)



Figure: MATLAB simulation result of Odd Parity Checker where B<sub>3</sub> B<sub>2</sub> B<sub>1</sub> B<sub>0</sub> P varies from 10000 to 11111

Dr. Santosh Kumar

## Design of BCD to Excess-3 code converter

Santosh Kumar et. al., Frontier in Optics/Laser sources (FiO/LS-2016), paper JW4A.33, Rochester, New York, United States, 17-21 October 2016.



Figure: Schematic diagram of BCD to excess 3 code converter

#### MATLAB Results for BCD to Excess 3 code converter



Figure: MATLAB simulation result of BCD to Excess-3 code converter where B<sub>3</sub> B<sub>2</sub> B<sub>1</sub> B<sub>0</sub> varies from 0000 to 0100

#### **BPM Simulation Result**



Figure: BPM result of BCD to Excess-3 code converter where  $B_3 B_2 B_1 B_0$  varies from 0000 to 1001

Dr. Santosh Kumar

### Design of Excess 3 to BCD code converter

**Santosh Kumar** et. al., Proc. SPIE 9889, Optical Modelling and Design IV, SPIE Photonics Europe 2016, **Brussels, Belgium**, PP. 98890E (April 4-7, 2016).

#### Excess-3 to BCD code converter



Figure: Digital circuits and Schematic diagram of K-map of excess 3 to BCD code converter.

#### Excess-3 to BCD code converter



Dr. Santosh Kumar

## Mathematical Expression for Excess 3 to BCD code converter

P<sub>0</sub>, P<sub>1</sub>, P<sub>2</sub>, P<sub>3</sub> is output power calculated for B<sub>0</sub>, B<sub>1</sub>, B<sub>2</sub>, B<sub>3</sub> respectively.

$$\begin{split} P_{0} &= \cos^{2}\left(\frac{\Delta\phi_{MZI1}}{2}\right) \\ P_{1} &= \sin^{2}\left(\frac{\Delta\phi_{MZI2}}{2}\right)\cos^{2}\left(\frac{\Delta\phi_{MZI3}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI2}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI3}}{2}\right) \\ P_{2} &= \cos^{2}\left(\frac{\Delta\phi_{MZI4}}{2}\right)\cos^{2}\left(\frac{\Delta\phi_{MZI5}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI6}}{2}\right)\cos^{2}\left(\frac{\Delta\phi_{MZI7}}{2}\right) \\ &+ \sin^{2}\left(\frac{\Delta\phi_{MZI8}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI9}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI10}}{2}\right) \\ P_{3} &= \sin^{2}\left(\frac{\Delta\phi_{MZI11}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI12}}{2}\right) \\ &+ \sin^{2}\left(\frac{\Delta\phi_{MZI13}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI14}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI15}}{2}\right) \\ \end{split}$$

#### MATLAB Results for Excess 3 to BCD code converter



Figure: MATLAB simulation result of Excess 3 to BCD code converter where  $E_3 E_2 E_1 E_0$  varies from 0011 to 0101 Dr. Santosh Kumar

#### Contd..



Figure: MATLAB simulation result of Excess 3 to BCD code converter where  $E_3 E_2 E_1 E_0$  varies from 0110 to 1000

Contd..



Figure: MATLAB simulation result of Excess 3 to BCD code converter where  $E_3 E_2 E_1 E_0$  varies from 1001 to 1100 Dr. Santosh Kumar

#### BPM Layout of Excess 3 to code converter



Figure: BPM layout of Excess-3 to BCD code converter

#### **BPM Simulation Result**



Figure: BPM result of Excess 3 to BCD code converter where E<sub>3</sub> E<sub>2</sub> E<sub>1</sub> E<sub>0</sub> varies from 0011 to 1100



### Design of Transmission gate

Santosh Kumar et. al., Photonic Network communications (Springer), Vol. 33, PP. 1-9, (Mar. 24, 2017).

#### Transmission gate



Figure: Digital circuit of transmission gate



Truth table and mathematical expression for Transmission gate

output = 
$$\left[ sin^2 \left( \frac{\Delta \emptyset_{MZI1}}{2} \right) cos^2 \left( \frac{\Delta \emptyset_{MZI3}}{2} \right) + cos^2 \left( \frac{\Delta \emptyset_{MZI1}}{2} \right) sin^2 \left( \frac{\Delta \emptyset_{MZI2}}{2} \right) \right] sin^2 \left( \frac{\Delta \emptyset_{MZI4}}{2} \right)$$

Control	Input	Output
Signal	signal	Signal
Ē	Α	Output
0	0	0
0	1	0
1	0	0
1	1	1

#### **MATLAB Simulation Results**



Figure: MATLAB simulation result of transmission gate where C, A varies from 00 to 11



gate.

Figure: Schematic diagram of 2 x 1 multiplexer using transmission gate



## Truth table and mathematical expression for 2x1 multiplexer using Transmission gate

$$\text{output} = \left[ \sin^2 \left( \frac{\Delta \phi_{MZI1}}{2} \right) \ \cos^2 \left( \frac{\Delta \phi_{MZI3}}{2} \right) + \cos^2 \left( \frac{\Delta \phi_{MZI1}}{2} \right) \ \sin^2 \left( \frac{\Delta \phi_{MZI2}}{2} \right) \right] \ \sin^2 \left( \frac{\Delta \phi_{MZI4}}{2} \right) \\ + \left[ \sin^2 \left( \frac{\Delta \phi_{MZI6}}{2} \right) \ \sin^2 \left( \frac{\Delta \phi_{MZI7}}{2} \right) + \cos^2 \left( \frac{\Delta \phi_{MZI6}}{2} \right) \ \cos^2 \left( \frac{\Delta \phi_{MZI8}}{2} \right) \right] \ \sin^2 \left( \frac{\Delta \phi_{MZI9}}{2} \right)$$

Control	Input signal		Output signal
signal			
$\overline{C}$	B	Α	Output
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

#### MATLAB Simulation Results of 2x1 multiplexer



Dr. Santosh Kumar

C, B, A varies from a 000 to 01. b 100 to 111



Figure: Simulation results of transmission gate where C, A varies from 00 to 11 obtained through beam propagation method.



#### Simulation Result of 2x1 multiplexer



Figure: Simulation result of transmission gate where C, B, A varies from 000 to 111 obtained through beam propagation method Dr. Santosh Kumar

# Design of binary to octal and octal to binary code converter

<u>Santosh Kumar</u> et al., Journal of Optical Communications (Degruyter), DOI: 10.1515/joc-2016-N055, August 2016.



Design of binary to octal and octal to binary code converter

- ➢ Binary to octal and octal to binary code converter is a device that allows placing digital information from many inputs to many outputs.
- ➢ Binary to octal code converter accepts three binary inputs (A, B and C) and produces eight octal outputs ( $O_0, O_1, O_2, O_3, O_4, O_5, O_6, \text{and } O_7$ ).

> Octal to binary code converter accepts eight inputs  $(I_0, I_1, I_2, I_3, I_4, I_5, I_6, \text{ and } I_7)$  and produces three binary outputs  $(B_0, B_1 \text{ and } B_2)$ .



Figure: Schematic diagram of binary to octal code converter using MZIs
# Mathematical Expression for binary to octal code converter

Normalized power at the output ports

 $(O_0, O_1, O_2, O_3, O_4, O_5, O_6, \text{ and } O_7)$  are calculated using the mathematical expression as:

The output  $O_0$  at second output port of MZI4 as  $O_0 = \cos^2\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\cos^2\left(\frac{\Delta\varphi_{MZI2}}{2}\right)\cos^2\left(\frac{\Delta\varphi_{MZI4}}{2}\right)$ The output  $O_1$  at first output port of MZI4 as;  $O_1 = \cos^2\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\cos^2\left(\frac{\Delta\varphi_{MZI2}}{2}\right)\sin^2\left(\frac{\Delta\varphi_{MZI4}}{2}\right)$ The output  $O_2$  at second output port of MZI5 as;  $O_2 = \cos^2\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\sin^2\left(\frac{\Delta\varphi_{MZI2}}{2}\right)\cos^2\left(\frac{\Delta\varphi_{MZI5}}{2}\right)$ 

#### Cont....

The output  $O_3$  at first output port of MZI5 as;  $O_3 = \cos^2\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\sin^2\left(\frac{\Delta\varphi_{MZI2}}{2}\right)\sin^2\left(\frac{\Delta\varphi_{MZI5}}{2}\right)$ The output  $O_4$  at second output port of MZI6 as;  $O_4 = \sin^2\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\cos^2\left(\frac{\Delta\varphi_{MZI3}}{2}\right)\cos^2\left(\frac{\Delta\varphi_{MZI6}}{2}\right)$ The output  $O_5$  at first output port of MZI6 as;  $O_{5} = \sin^{2}\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\cos^{2}\left(\frac{\Delta\varphi_{MZI3}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI6}}{2}\right)$ The output  $O_6$  at second output port of MZI7 as;  $O_6 = \sin^2\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\sin^2\left(\frac{\Delta\varphi_{MZI3}}{2}\right)\cos^2\left(\frac{\Delta\varphi_{MZI7}}{2}\right)$ The output  $O_7$  at first output port of MZI7 as;  $O_7 = \sin^2\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\sin^2\left(\frac{\Delta\varphi_{MZI3}}{2}\right)\sin^2\left(\frac{\Delta\varphi_{MZI7}}{2}\right)$ 

Dr. Santosh Kumar

# MATLAB simulation Results of binary to octal code converter



Figure: MATLAB simulation result for (a) ABC=000 to 011 of B-O code converter (b) ABC=100 to 111 of B-O code converter

Dr. Santosh Kumar

#### Cont....



Figure: Schematic diagram of 112 ctal torbinaryh code converter

#### Table: Truth table of binary to octal code converter

Bin	ary in	put	Octal Output							
Α	В	С	<i>O</i> <sub>0</sub>	$O_1$	02	03	$O_4$	05	06	07
0	0	0	1	0	0	0	0	0	0	0
0	0	1	0	1	0	0	0	0	0	0
0	1	0	0	0	1	0	0	0	0	0
0	1	1	0	0	0	1	0	0	0	0
1	0	0	0	0	0	0	1	0	0	0
1	0	1	0	0	0	0	0	1	0	0
1	1	0	0	0	0	0	0	0	1	0
1	1	1	0	0	0	0	0	0	0	1

Table: Truth table of octal to binary code converter

		0	ctal	Bina	ary ou	tput				
I <sub>0</sub>	$I_1$	$I_2$	$I_3$	$I_4$	$I_5$	$I_6$	$I_7$	<i>B</i> <sub>2</sub>	$B_1$	$B_0$
1	0	0	0	0	0	0	0	0	0	0
0	1	0	0	0	0	0	0	0	0	1
0	0	1	0	0	0	0	0	0	1	0
0	0	0	1	0	0	0	0	0	1	1
0	0	0	0	1	0	0	0	1	0	0
0	0	0	0	0	1	0	0	1	0	1
0	0	0	0	0	0	1	0	1	1	0
0	0	0	0	0	0	0	1	1	1	1

# Mathematical Expression for octal to binary code converter

Normalized power at output ports are computed using the mathematical expression as:

$$B_{0} = \sin^{2}\left(\frac{\Delta\varphi_{MZI1}}{2}\right) + \sin^{2}\left(\frac{\Delta\varphi_{MZI3}}{2}\right) + \sin^{2}\left(\frac{\Delta\varphi_{MZI5}}{2}\right) + \sin^{2}\left(\frac{\Delta\varphi_{MZI7}}{2}\right)$$
$$B_{1} = \sin^{2}\left(\frac{\Delta\varphi_{MZI2}}{2}\right) + \sin^{2}\left(\frac{\Delta\varphi_{MZI3}}{2}\right) + \sin^{2}\left(\frac{\Delta\varphi_{MZI6}}{2}\right) + \sin^{2}\left(\frac{\Delta\varphi_{MZI7}}{2}\right)$$
$$B_{2} = \sin^{2}\left(\frac{\Delta\varphi_{MZI4}}{2}\right) + \sin^{2}\left(\frac{\Delta\varphi_{MZI5}}{2}\right) + \sin^{2}\left(\frac{\Delta\varphi_{MZI6}}{2}\right) + \sin^{2}\left(\frac{\Delta\varphi_{MZI7}}{2}\right)$$

#### Cont....



Figure: MATLAB simulation result for (a) input  $I_0$  to  $I_3$  (b) input  $I_4$  to  $I_7$ 



#### BPM results of binary to octal code converter



Figure: Results of binary to octal code converter for different combinations of control signals obtained through beam propagation method Dr. Santosh Kumar

#### BPM results of octal to binary code converter



Figure: BPM simulation results for octal to binary code conversion from  $I_0$  to  $I_7$ 

## Design of Optical Boolean function generator

Santosh Kumar et. al., Journal of Optical Communications (Degruyter), DOI: 10.1515/joc-

2016-0080, July 2016.

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Dr. Santosh Kumar

Design of optical Boolean function generator

- Optical Boolean function generator unit can generates multiple logical operations.
- This design have two parts: one part is decoder circuit and other part is logic selection unit.
- ➤ A continuous wave (CW) optical signal is applied at second input port of MZI1.

#### Cont...



Figure: Schematic diagram of Boolean function generator unit

#### Cont...

Table: Generation of Boolean logical operation using generator unit for different control signal (*P*, *Q*, *R*, and *S*)

S	S Select Control Signal			l Signal	Output of the function generator unit					
No.	Р	Q	R	S	0,	<b>0</b> <sub>2</sub>				
1	0	0	0	0	1 (High Logic)	0 (Low Logic)				
2	0	0	0	1	$(\bar{A}\bar{B} + \bar{A}B + A\bar{B}) = \bar{A} + \bar{B}$	AB				
3	0	0	1	0	$(\bar{A}\bar{B} + \bar{A}B + AB) = \bar{A} + B$	$A\overline{B}$				
4	0	0	1	1	$(\bar{A}\bar{B} + \bar{A}B) = \bar{A}$	$(A\overline{B} + AB) = A$				
5	0	1	0	0	$(\bar{A}B + A\bar{B} + AB) = A + B$	$ar{A}ar{B}$				
6	0	1	0	1	$(\bar{A}B + A\bar{B}) = A \mathbf{\Phi}B$	$(\bar{A}\bar{B} + AB) = A\mathbf{O}B$				
7	0	1	1	0	$(\bar{A}B + AB) = B$	$(\bar{A}\bar{B} + A\bar{B}) = \bar{B}$				
8	0	1	1	1	$\bar{AB}$	$(\bar{A}\bar{B} + A\bar{B} + AB) = A + \bar{B}$				
9	1	0	0	0	$(\bar{A}\bar{B} + A\bar{B} + AB) = A + \bar{B}$	ĀB				
10	1	0	0	1	$(\bar{A}\bar{B} + A\bar{B}) = \bar{B}$	$(\bar{A}B + AB) = B$				
11	1	0	1	0	$(\bar{A}\bar{B} + AB) = A\mathbf{O}B$	$(\bar{A}B + A\bar{B}) = A \mathbf{\Phi}B$				
12	1	0	1	1	$ar{A}ar{B}$	$(\bar{A}B + A\bar{B} + AB) = A + B$				
13	1	1	0	0	$(A\overline{B} + AB) = A$	$(\bar{A}\bar{B} + \bar{A}B) = \bar{A}$				
14	1	1	0	1	$A\overline{B}$	$(\bar{A}\bar{B} + \bar{A}B + AB) = \bar{A} + B$				
15	1	1	1	0	AB	$(\overline{A}\overline{B} + \overline{A}B + A\overline{B}) = \overline{A} + \overline{B}$				
16	1	1	1	1	0 (Low Logic)	1 (High Logic)				

Mathematical Expression for optical Boolean function generator

Using output at single stage MZI, we can write the mathematical expression to obtain optical signal at the output ports  $O_1, O_2$  $O_1 = \begin{cases} \cos^2\left(\frac{\Delta \phi_{MZI1}}{2}\right) \sin^2\left(\frac{\Delta \phi_{MZI2}}{2}\right) \cos^2\left(\frac{\Delta \phi_{MZI4}}{2}\right) \\ +\cos^2\left(\frac{\Delta \phi_{MZI1}}{2}\right) \cos^2\left(\frac{\Delta \phi_{MZI2}}{2}\right) \cos^2\left(\frac{\Delta \phi_{MZI5}}{2}\right) \\ +\sin^2\left(\frac{\Delta \phi_{MZI1}}{2}\right) \cos^2\left(\frac{\Delta \phi_{MZI3}}{2}\right) \cos^2\left(\frac{\Delta \phi_{MZI6}}{2}\right) \\ +\sin^2\left(\frac{\Delta \phi_{MZI1}}{2}\right) \sin^2\left(\frac{\Delta \phi_{MZI3}}{2}\right) \cos^2\left(\frac{\Delta \phi_{MZI7}}{2}\right) \end{bmatrix}$  Cont...

$$O_{2} = \begin{bmatrix} \cos^{2}\left(\frac{\Delta \emptyset_{MZI1}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI2}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI4}}{2}\right) \\ +\cos^{2}\left(\frac{\Delta \emptyset_{MZI1}}{2}\right) \cos^{2}\left(\frac{\Delta \emptyset_{MZI2}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI5}}{2}\right) \\ +\sin^{2}\left(\frac{\Delta \emptyset_{MZI1}}{2}\right) \cos^{2}\left(\frac{\Delta \emptyset_{MZI3}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI6}}{2}\right) \\ +\sin^{2}\left(\frac{\Delta \emptyset_{MZI1}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI3}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI7}}{2}\right) \end{bmatrix}$$



Figure: MATLAB simulation results for different combinations of AB at PQRS=0000



Dr. Santosh Kumar



### Design of 1's and 2's complement device

Santosh Kumar et. al., Optical Engineering (SPIE), Vol. 55, Issue 12, pp. 125104 (Dec 20, 2016).



#### Optical 1's and 2's complement device



Table: Truth table of 1's complement device										
E	Binary	y inpu	ıt	1's	1's complement					
(4	bit n	umbe	r)			-				
Α	В	С	D	Р	Q	R	S			
0	0	0	0	1	1	1	1			
0	0	0	1	1	1	1	0			
0	0	1	0	1	1	0	1			
0	0	1	1	1	1	0	0			
0	1	0	0	1	0	1	1			
0	1	0	1	1	0	1	0			
0	1	1	0	1	0	0	1			
0	1	1	1	1	0	0	0			
1	0	0	0	0	1	1	1			
1	0	0	1	0	1	1	0			
1	0	1	0	0	1	0	1			
1	0	1	1	0	1	0	0			
1	1	0	0	0	0	1	1			
1	1	0	1	0	0	1	0			
1	1	1	0	0	0	0	1			
1	1	1	1	0	0	0	0			

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Figure: Schematic diagram of 1's complement using MZIs

#### Mathematical Expression for 1's complement device

Normalized power at second output port of MZI1 is written as;

$$P = \cos^2\left(\frac{\Delta\varphi_{MZI1}}{2}\right)$$

Normalized power at second output port of MZI2

$$Q = \cos^2\left(\frac{\Delta\varphi_{MZI2}}{2}\right)$$

Normalized power at second output port of MZI3

$$R = \cos^2\left(\frac{\Delta\varphi_{MZI3}}{2}\right)$$

Normalized power at second output port of MZI4

$$S = \cos^2\left(\frac{\Delta\varphi_{MZI4}}{2}\right)$$



#### MATLAB simulation Results of 1's complement device



Figure: MATLAB simulation result of 1's complement for different ABCD (0000 – 0011)



#### 2's complement device



Figure: Schematic layout of 2's complement device

Table: Truth table of 2's complement device										
]	Binary	y inpu	t	2's complement						
(4	bit n	umber	()			_				
Α	В	С	D	E	F	G	Η			
0	0	0	0	0	0	0	0			
0	0	0	1	1	1	1	1			
0	0	1	0	1	1	1	0			
0	0	1	1	1	1	0	1			
0	1	0	0	1	1	0	0			
0	1	0	1	1	0	1	1			
0	1	1	0	1	0	1	0			
0	1	1	1	1	0	0	1			
1	0	0	0	1	0	0	0			
1	0	0	1	0	1	1	1			
1	0	1	0	0	1	1	0			
1	0	1	1	0	1	0	1			
1	1	0	0	0	1	0	0			
1	1	0	1	0	0	1	1			
1	1	1	0	0	0	1	0			
1	1	1	1	0	0	0	1			

Mathematical Expression for 2's complement device

Normalized power at second output port of MZI4 is given as

$$E = \begin{bmatrix} \left\{ \sin^2 \left( \frac{\Delta \varphi_{MZI1}}{2} \right) + \sin^2 \left( \frac{\Delta \varphi_{MZI2}}{2} \right) + \sin^2 \left( \frac{\Delta \varphi_{MZI3}}{2} \right) \right\} \cos^2 \left( \frac{\Delta \varphi_{MZI4}}{2} \right) + \\ \left\{ \cos^2 \left( \frac{\Delta \varphi_{MZI1}}{2} \right) + \cos^2 \left( \frac{\Delta \varphi_{MZI2}}{2} \right) + \cos^2 \left( \frac{\Delta \varphi_{MZI3}}{2} \right) \right\} \\ \left\{ \cos^2 \left( \frac{\Delta \varphi_{MZI1}}{2} \right) \cos^2 \left( \frac{\Delta \varphi_{MZI2}}{2} \right) \cos^2 \left( \frac{\Delta \varphi_{MZI3}}{2} \right) \right\} \sin^2 \left( \frac{\Delta \varphi_{MZI4}}{2} \right) \end{bmatrix} \end{bmatrix}$$

#### Cont....

Normalized power at second output port of MZI5 is given as

$$F = \begin{bmatrix} \left\{ \sin^2 \left( \frac{\Delta \varphi_{MZI2}}{2} \right) + \sin^2 \left( \frac{\Delta \varphi_{MZI3}}{2} \right) \right\} \cos^2 \left( \frac{\Delta \varphi_{MZI5}}{2} \right) + \\ \left\{ \cos^2 \left( \frac{\Delta \varphi_{MZI2}}{2} \right) + \cos^2 \left( \frac{\Delta \varphi_{MZI3}}{2} \right) \right\} \\ \left\{ \cos^2 \left( \frac{\Delta \varphi_{MZI2}}{2} \right) \cos^2 \left( \frac{\Delta \varphi_{MZI3}}{2} \right) \right\} \sin^2 \left( \frac{\Delta \varphi_{MZI5}}{2} \right) \end{bmatrix} \end{bmatrix}$$

Normalized power at second output port of MZI6 is given as

$$G = \begin{bmatrix} \left\{ \sin^2 \left( \frac{\Delta \varphi_{MZI3}}{2} \right) \right\} \cos^2 \left( \frac{\Delta \varphi_{MZI6}}{2} \right) + \\ \left\{ \cos^2 \left( \frac{\Delta \varphi_{MZI3}}{2} \right) \right\} \sin^2 \left( \frac{\Delta \varphi_{MZI6}}{2} \right) \end{bmatrix}$$

Normalized power at first output port of MZI7 is given as

$$H = \sin^2\left(\frac{\Delta\varphi_{MZI3}}{2}\right)$$

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### MATLAB simulation Results of 2's complement device



Figure: MATLAB simulation result of 2's complement for differentABCD (0000 - 0011)



#### BPM results of 2's complement device



Figure 34: BPM simulation result of 2's complement device for different control signal ABCD (0000 - 0011)



### Design of Decoder and Encoder Device

Santosh Kumar et. al., Photonics Network Communication (Springer), (2017) DOI: 10.1007/s11107-017-0718-8

Dr. Santosh Kumar

#### Design of 2 to 4 line Decoder

- Decoder is a device that allows placing digital information from many inputs to many outputs.
- Any application of combinational logic circuit can be implemented by using decoder and external gates.



Table 2: Truth table of 2 to 4 line decoder

		C	ontrol	Signals	Optical propagation at output ports			
	E	A B Output O		Output O <sub>0</sub>	Output O <sub>1</sub>	Output O <sub>2</sub>	Output O <sub>3</sub>	
	0	Х	Х	0	0	0	0	
	1	0	0	1	0	0	0	
	1	0	1	0	1	0	0	
Dr. Santosh Kuma	r 1	1	0	0	0	1	0	
	1	1	1	0	0	0	1	

#### Mathematical Expression for 2 to 4 line decoder

We can write the output  $O_0$  at second output port of MZI3 as;

$$O_{0} = \left| \frac{O_{0}_{MZI3}}{E_{in}} \right|^{2} = \sin^{2} \left( \frac{\Delta \phi_{MZI1}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{MZI2}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{MZI3}}{2} \right)$$
(8)  

$$O_{1} = \left| \frac{O_{1}_{MZI3}}{E_{in}} \right|^{2} = \sin^{2} \left( \frac{\Delta \phi_{MZI1}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{MZI2}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{MZI3}}{2} \right)$$
(9)  

$$O_{2} = \left| \frac{O_{2}_{MZI4}}{E_{in}} \right|^{2} = \sin^{2} \left( \frac{\Delta \phi_{MZI1}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{MZI2}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{MZI4}}{2} \right)$$
(10)  

$$O_{3} = \left| \frac{O_{3}_{MZI4}}{E_{in}} \right|^{2} = \sin^{2} \left( \frac{\Delta \phi_{MZI1}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{MZI2}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{MZI4}}{2} \right)$$
(11)

#### MATLAB simulation Results of 2 to 4 line decoder



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#### BPM Layout of 2 to 4 line decoder



Figure 7: Layout of 2 to 4 line decoder



Figure 8: Results of 2 to 4 line decoder for different combinations of control signals (*E*, *A* and *B*)

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obtained through beam propagation method



Figure 9: Schematic digram of 3 to 8 lineoptical decoder

#### Mathematical Expression for 3 to 8 Line Decoder

The output  $O_0$  at second output port of MZI5 as;

$$O_0 = \left| \frac{O_{0_{MZI5}}}{E_{in}} \right|^2 = \sin^2 \left( \frac{\Delta \phi_{MZI1}}{2} \right) \cos^2 \left( \frac{\Delta \phi_{MZI2}}{2} \right) \cos^2 \left( \frac{\Delta \phi_{MZI3}}{2} \right) \cos^2 \left( \frac{\Delta \phi_{MZI5}}{2} \right)$$
(12)

The output  $O_1$  at first output port of MZI5 as;

$$O_{1} = \left| \frac{O_{1_{\text{MZI}5}}}{E_{\text{in}}} \right|^{2} = \sin^{2} \left( \frac{\Delta \phi_{MZI1}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{MZI2}}{2} \right) \cos^{2} \left( \frac{\Delta \phi_{MZI3}}{2} \right) \sin^{2} \left( \frac{\Delta \phi_{MZI5}}{2} \right)$$
(13)

The output  $O_2$  at second output port of MZI6 as;

$$O_2 = \left| \frac{O_{2_{MZI6}}}{E_{in}} \right|^2 = \sin^2 \left( \frac{\Delta \phi_{MZI1}}{2} \right) \cos^2 \left( \frac{\Delta \phi_{MZI2}}{2} \right) \sin^2 \left( \frac{\Delta \phi_{MZI3}}{2} \right) \cos^2 \left( \frac{\Delta \phi_{MZI6}}{2} \right)$$
(14)

The output  $O_3$  at first output port of MZI6 as;

$$O_{3} = \left| \frac{O_{3_{MZI6}}}{E_{in}} \right|^{2} = sin^{2} \left( \frac{\Delta \phi_{MZI1}}{2} \right) cos^{2} \left( \frac{\Delta \phi_{MZI2}}{2} \right) sin^{2} \left( \frac{\Delta \phi_{MZI3}}{2} \right) sin^{2} \left( \frac{\Delta \phi_{MZI6}}{2} \right)$$
(15)

#### Cont....

The output  $O_4$  at second output port of MZI7 as

$$O_4 = \left| \frac{O_{4_{\text{MZI7}}}}{E_{\text{in}}} \right|^2 = \sin^2 \left( \frac{\Delta \phi_{MZI1}}{2} \right) \sin^2 \left( \frac{\Delta \phi_{MZI2}}{2} \right) \cos^2 \left( \frac{\Delta \phi_{MZI4}}{2} \right) \cos^2 \left( \frac{\Delta \phi_{MZI7}}{2} \right) \tag{16}$$

The output  $O_5$  at first output port of MZI7 as

$$O_{5} = \left|\frac{O_{5_{MZI7}}}{E_{in}}\right|^{2} = sin^{2} \left(\frac{\Delta \phi_{MZI1}}{2}\right) sin^{2} \left(\frac{\Delta \phi_{MZI2}}{2}\right) cos^{2} \left(\frac{\Delta \phi_{MZI4}}{2}\right) sin \left(\frac{\Delta \phi_{MZI7}}{2}\right)$$
(17)

The output  $O_6$  at second output port of MZI8 as

$$O_{6} = \left| \frac{O_{6_{MZI8}}}{E_{in}} \right|^{2} = sin^{2} \left( \frac{\Delta \emptyset_{MZI1}}{2} \right) sin^{2} \left( \frac{\Delta \emptyset_{MZI2}}{2} \right) sin^{2} \left( \frac{\Delta \emptyset_{MZI4}}{2} \right) cos^{2} \left( \frac{\Delta \emptyset_{MZI8}}{2} \right)$$
(18)

The output  $O_7$  at first output port of MZI8 as

$$O_7 = \left| \frac{O_{7_{\text{MZI8}}}}{E_{\text{in}}} \right|^2 = \sin^2 \left( \frac{\Delta \emptyset_{MZI1}}{2} \right) \sin^2 \left( \frac{\Delta \emptyset_{MZI2}}{2} \right) \sin^2 \left( \frac{\Delta \emptyset_{MZI4}}{2} \right)$$
#### BPM Layout of 3 to 8 Line Decoder MZI1 MZI2 MZI4 MZI3 MZI8MZI7 (E) (A) (B) (B) (C) (C) →Output Port O7 →Output Port O6 →Output Port O5 Optical Signal→ →Output Port O4 →Output Port O3 →Output Port O2 →Output Port O1 -Output Port On MZI6MZI5 (C) (C) Figure 10: Layout diagram of 3 to 8 line decoder E A В C 00 01 02 03 04 05 06 07 В 00 01 02 03 04 05 06 07 E. A C Port O 6 Optical Signal → Port O 5 0 Optical Signal → 0 Port O 4 Port 0.4 Port 0.3 Port 0.2 Port 0.1 Port 0.0 Optical Signal → 0 Port O 6 Port O 5 Optical Signal → 0 0 0 Port O 4 Port O 3 Port O 2 Port O 1 0 Port O 0 Optical Signal → Port O 7 Port O Port O 5 Optical Signal -> Port O 4 0 0 1 0 11 1 0 Port O3 Port O 2 Port O 1 Optical Signal -> Port O 0 Port O Port O 5 Optical Signal → Port O 4 0 0 0 0 0 0 0 1 1 1 1 1 Port O 2 Port O 1 0 1 Optical Signal → 1 0 0

Figure 11 (a): Simulation results of 3 to 8 line decoder forcontrol signals E, A, B and C is 1000 to Figure 11 (b): Simulation results of 3 to 8 line decoder forcontrol signals E, A, B and C is 1100 to

Dr. SouttobstainEduthrough beam propagation method

1111 obtained through beam propagation method

# Design of 4 to 2 line Encoder

Santosh Kumar et. al., Proc. SPIE 9889, Optical Modelling and Design IV, 98890H Brussels, Belgium 2016.

Dr. Santosh Kumar

## Design of 4 to 2 line Encoder



Figure 12: Schematic diagram of 4 to 2 Line Encoder using MZIs

Table 4: Truth table of 4 to 2 line Encoder

<b>Control Signals</b>					Output at different Ports		
E	I <sub>0</sub>	I <sub>1</sub>	I <sub>2</sub>	I <sub>3</sub>	Output (O <sub>1</sub> )	Output (O <sub>0</sub> )	
1	1	0	0	0	0	0	
1	0	1	0	0	0	1	
1	0	0	1	0	1	0	
1	0	0	0	1	1	1	

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## Mathematical Expression for 4 to 2 Line Encoder

To operate 4 to 2 line encoder, the power appears at second output port of MZI5 and MZI6. So the normalized power at the second output port is computed as follows:

$$O_{0} = \sin^{2}\left(\frac{\Delta \emptyset_{MZI1}}{2}\right) \cos^{2}\left(\frac{\Delta \emptyset_{MZI5}}{2}\right) + \sin^{2}\left(\frac{\Delta \emptyset_{MZI2}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI5}}{2}\right) + \sin^{2}\left(\frac{\Delta \emptyset_{MZI4}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI5}}{2}\right)$$
(20)

$$O_1 = \sin^2\left(\frac{\Delta \phi_{MZI3}}{2}\right) \sin^2\left(\frac{\Delta \phi_{MZI6}}{2}\right) + \sin^2\left(\frac{\Delta \phi_{MZI4}}{2}\right) \sin^2\left(\frac{\Delta \phi_{MZI6}}{2}\right)$$
(21)

## MATLAB simulation Results of 4 to 2 Line Encoder



Dr. Santosh Kumar Figure 13: MATLAB simulation result of 4 to 2 Line Encoder

## BPM layout and results of 4 to 2 Line Encoder



Figure 14 (a): OptiBPM layout diagram of 4 to 2 Line Encoder



Figure 14 (b): OptiBPM simulation results for 4 to 2 Line Encoder

Dr. Santosh Kumar

## Design of Four-Bit Priority Encoder using MZIs

<u>Santosh Kumar</u>, et. al., IEEE/Workshop on Recent Advances in Photonics 2015, Indian Institute of Science, Bangalore, India, 16-17 Dec., 2015 (IEEE Xplore).

Dr. Santosh Kumar

## Design of Four-Bit Priority Encoder using MZIs



Figure 22: Schematic diagram of 4-bit priority encoder using MZIs

#### Mathematical expression of Four-Bit Priority Encoder

The proper combination of minterms provides the expression for the output of the priority encoder. The expression for valid-bit (V) can be written as

$$V = \sin^2\left(\frac{\Delta\phi_{MZI\,1}}{2}\right) + \sin^2\left(\frac{\Delta\phi_{MZI\,2}}{2}\right) + \sin^2\left(\frac{\Delta\phi_{MZI\,4}}{2}\right) + \sin^2\left(\frac{\Delta\phi_{MZI\,5}}{2}\right)$$
(30)

Similarly x and y can be represented as

$$x = \sin^{2}\left(\frac{\Delta\phi_{MZI4}}{2}\right) + \sin^{2}\left(\frac{\Delta\phi_{MZI5}}{2}\right)$$
(31)  
$$y = \sin^{2}\left(\frac{\Delta\phi_{MZI4}}{2}\right) + \sin^{2}\left(\frac{\Delta\phi_{MZI2}}{2}\right) \cos^{2}\left(\frac{\Delta\phi_{MZI3}}{2}\right)$$
(32)

Where,

$$\begin{aligned} \phi_{0MZI\,1} &= \frac{\phi_{1MZI\,1} + \phi_{2MZI\,1}}{2} \\ \phi_{0MZI\,2} &= \frac{\phi_{1MZI\,2} + \phi_{2MZI\,2}}{2} \\ \phi_{0MZI\,3} &= \frac{\phi_{1MZI\,3} + \phi_{2MZI\,3}}{2} \\ \phi_{0MZI\,4} &= \frac{\phi_{1MZI\,4} + \phi_{2MZI\,4}}{2} \\ \phi_{0MZI\,5} &= \frac{\phi_{1MZI\,5} + \phi_{2MZI\,5}}{2} \end{aligned} \right\} \\ \begin{aligned} \Delta \phi_{MZI\,2} &= \phi_{1MZI\,3} - \phi_{2MZI\,2} &= \frac{\pi}{V_{\pi}} D_{1} \\ \Delta \phi_{MZI\,3} &= \phi_{1MZI\,3} - \phi_{2MZI\,3} &= \frac{\pi}{V_{\pi}} D_{2} \\ \Delta \phi_{MZI\,4} &= \phi_{1MZI\,4} - \phi_{2MZI\,4} &= \frac{\pi}{V_{\pi}} D_{3} \\ \Delta \phi_{MZI\,5} &= \phi_{1MZI\,5} - \phi_{2MZI\,5} &= \frac{\pi}{V_{\pi}} D_{2} \end{aligned}$$

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#### ATLAB Result of Four-Bit Priority Encoder D3 (Volts) D2 (Volts) D1 (Volts) D0 (Volts) × 0.5 > 0.5 0.5 > Time (µs) D3 (Volts) D1 (Volts) D2 (Volts) D0 (Volts) > 0.5 0.5 0.5 × > Time (µs) (Volts) D3 (Volts) D1 (Volts) (Volts) > 0.5 × 0.5 0.5 > D2 DO Time (µs) D3 (Volts) D2 (Volts) D0 (Volts) D1 (Volts) > 0.5 × 0.5 0.5 >



Figure 23: MATLAB Simulation results of four-bit priority encoder for different combinations of data signals. Dr. Santosh Kumar

#### BPM Result of Four-Bit Priority Encoder

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Figure 24: Results of four-bit priority encoder for different combinations of data signals obtained through BPM.

# Design of Optical seven segment decoder

Santosh Kumar et. al., Optical Engineering (SPIE), Vol. 56, Issue 1, pp. 017103 (Jan 06,

2017).

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Dr. Santosh Kumar

## Design of Seven Segment Decoder

- Seven segment decoder is a device that allows placing digital information from many inputs to many outputs optically.
- Conventional seven segment decoder having seven LED for showing the decimal digit 0 to 9. Each LED require around 20mA current for their operation, so one seven segment decoder requires 140mA current.

### Cont....

 $\begin{array}{c}
c_0\\
c_1\\
c_5\\
c_6\\
c_2\\
c_4\\
c_3
\end{array}$ 

Optical Signal

Optical Signal

Optical Signal

Optical Signal

Figure 35: structure of seven segment display

Α	B	С	D	C <sub>0</sub>	<b>C</b> <sub>1</sub>	<b>C</b> <sub>2</sub>	Сз	<b>C</b> 4	<b>C</b> 5	C <sub>6</sub>
0	0	0	0	1	1	1	1	1	1	0
0	0	0	1	0	1	1	0	0	0	0
0	0	1	0	1	1	0	1	1	0	1
0	0	1	1	1	1	1	1	0	0	1
0	1	0	0	0	1	1	0	0	1	1
0	1	0	1	1	0	1	1	0	1	1
0	1	1	0	1	0	1	1	1	1	1
0	1	1	1	1	1	1	0	0	0	0
1	0	0	0	1	1	1	1	1	1	1
1	0	0	1	1	1	1	1	0	1	1



Figure 36: Schematic layout diagram of seven segment decoder

Cont....



Figure 37: K Map for seven segment decoder

## Mathematical Expression for Seven Segment Device

Normalized power at output port  $C_0$  can be given as:

$$C_{0} = \sin^{2}\left(\frac{\Delta\phi_{MZI1}}{2}\right) + \sin^{2}\left(\frac{\Delta\phi_{MZI2}}{2}\right) + \sin^{2}\left(\frac{\Delta\phi_{MZI3}}{2}\right) \times \sin^{2}\left(\frac{\Delta\phi_{MZI5}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI3}}{2}\right) \times \cos^{2}\left(\frac{\Delta\phi_{MZI6}}{2}\right)$$

$$(43)$$

Normalized power at output port  $C_1$  is given as

$$C_{1} = \cos^{2}\left(\frac{\Delta\phi_{MZI3}}{2}\right) + \sin^{2}\left(\frac{\Delta\phi_{MZI2}}{2}\right) \times \sin^{2}\left(\frac{\Delta\phi_{MZI7}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI2}}{2}\right) \times \cos^{2}\left(\frac{\Delta\phi_{MZI8}}{2}\right)$$

$$(44)$$

Normalized power at output port  $C_2$  is given as

$$C_2 = \cos^2\left(\frac{\Delta\phi_{MZI2}}{2}\right) + \cos^2\left(\frac{\Delta\phi_{MZI3}}{2}\right) + \sin^2\left(\frac{\Delta\phi_{MZI4}}{2}\right)$$
(45)

Dr. Santosh Kumar

## Cont....

Normalized power at output port  $C_3$  is given as

$$C_{3} = \cos^{2}\left(\frac{\Delta\phi_{MZI3}}{2}\right) \times \sin^{2}\left(\frac{\Delta\phi_{MZI9}}{2}\right) + \sin^{2}\left(\frac{\Delta\phi_{MZI2}}{2}\right) \times \cos^{2}\left(\frac{\Delta\phi_{MZI7}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI3}}{2}\right) \times \cos^{2}\left(\frac{\Delta\phi_{MZI3}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI3}}{2}\right) \times \sin^{2}\left(\frac{\Delta\phi_{MZI8}}{2}\right)$$
(46)

Normalized power at output port  $C_4$  is given as

$$C_4 = \sin^2\left(\frac{\Delta\phi_{MZI2}}{2}\right) \times \cos^2\left(\frac{\Delta\phi_{MZI7}}{2}\right) + \cos^2\left(\frac{\Delta\phi_{MZI3}}{2}\right) \times \cos^2\left(\frac{\Delta\phi_{MZI6}}{2}\right)$$
(47)

Normalized power at output port  $C_5$  is given as

$$C_{5} = \sin^{2}\left(\frac{\Delta \emptyset_{MZI1}}{2}\right) + \cos^{2}\left(\frac{\Delta \emptyset_{MZI2}}{2}\right) \times \cos^{2}\left(\frac{\Delta \emptyset_{MZI8}}{2}\right) + \sin^{2}\left(\frac{\Delta \emptyset_{MZI3}}{2}\right) \times \cos^{2}\left(\frac{\Delta \emptyset_{MZI5}}{2}\right) + \cos^{2}\left(\frac{\Delta \emptyset_{MZI10}}{2}\right) \times \sin^{2}\left(\frac{\Delta \emptyset_{MZI3}}{2}\right)$$
(48)

Normalized power at output port  $C_6$  is given as

$$C_{6} = \sin^{2}\left(\frac{\Delta\phi_{MZI1}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI3}}{2}\right) \times \sin^{2}\left(\frac{\Delta\phi_{MZI9}}{2}\right) + \sin^{2}\left(\frac{\Delta\phi_{MZI2}}{2}\right) \times \cos^{2}\left(\frac{\Delta\phi_{MZI7}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI10}}{2}\right) \times \sin^{2}\left(\frac{\Delta\phi_{MZI3}}{2}\right)$$

$$(49)$$
Dr. Santosh Kumar

## BPM layout of Seven Segment device





Figure 39: Results of seven segment decoder for different combinations of control signals (ABCD = 0000) obtained through beam propagation method

## Design of Optical SR latch and flip flop

Santosh Kumar et. al., Journal of Optical Communications (2017).

Dr. Santosh Kumar

Design of SR Latch and Flip-Flop

- SR latch or flip flop can maintain a binary state indefinitely until directed by an input signal to switch state.
- Any application of sequential logic circuit can be implemented by using SR flip flop and external gates. Flip flop have two stable states.
- > It is also called binary or one bit storage memory element.

Cont....



## Cont....



Figure 41: Schematic diagram of SR Flip Flop

Та	Table 11: Functional table of SR latch						
S	R	$Q_{n+1}$	$\bar{Q}_{n+1}$	States			
0	0	$Q_n$	$ar{Q}_n$	Previous State			
0	1	0	1	Reset			
1	0	1	0	Set			
1	1	0	0	Invalid State			



## Mathematical Expression for SR Flip Flop

we can write the output  $Q_{n+1}$  at first output port of MZI4 as;

$$Q_{n+1} = \left|\frac{Q_{n+1_{\text{MZI4}}}}{E_{\text{in}}}\right|^2 = \sin^2\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\cos^2\left(\frac{\Delta\varphi_{MZI2}}{2}\right)\cos^2\left(\frac{\Delta\varphi_{MZI4}}{2}\right)$$
(50)

The output  $\overline{Q}_{n+1}$  at the first output port of MZI5 as:

$$\bar{Q}_{n+1} = \left| \frac{\bar{Q}_{n+1}}{E_{\text{in}}} \right|^2 = \sin^2 \left( \frac{\Delta \varphi_{MZI1}}{2} \right) \cos^2 \left( \frac{\Delta \varphi_{MZI3}}{2} \right) \cos^2 \left( \frac{\Delta \varphi_{MZI3}}{2} \right)$$
(51)

## MATLAB simulation Results of SR Flip-Flop



## BPM Layout of SR latch





Figure 44: BPM layout of SR flip-flop

## BPM results of SR Flip-Flop



$$Q_n = 0$$
 and  $Q_{n+1} = 0$ 

## Design of D and T Flip-flops

Santosh Kumar et. al., Applied Optics (OSA), Vol. 54, Issue 21, PP. 6397-6405 (July 20, 2015)

Dr. Santosh Kumar

## Design of D and T Flip-flops



Fig. 15: Schematic diagram of D flip-flop.

#### Table 4: Function table of D flip-flop.

$D_n$	CLK	Q <sub>n</sub>	$ar{Q}_n$
0	1	0	1
1	1	1	0
×	0	Last Q <sub>n</sub>	Last $\bar{Q}_n$

Fig. 16: Schematic diagram of T flip-flop.

#### Table 5: Function table of T flip-flop.

T <sub>m</sub>	Q <sub>m</sub>	$Q_{m+1}$	$\overline{\mathrm{Q}}_{\mathrm{m}}$	$\overline{Q}_{m+1}$
0	0	0	1	1
0	1	1	0	0
1	0	1	1	0
1	1	0	0	1



$$|Q_n|^2 = \sin^2\left(\frac{\Delta\varphi}{2}\right)|D_n|^2 + \cos^2\left(\frac{\Delta\varphi}{2}\right)|Q_{n-1}|^2 + |D_n| |Q_{n-1}| \sin \Delta\varphi$$
(17)

Similarly for  $\overline{Q}_n$  we can write,

$$|\bar{Q}_n|^2 = \sin^2\left(\frac{\Delta\varphi}{2}\right)|\bar{D}_n|^2 + \cos^2\left(\frac{\Delta\varphi}{2}\right)|\bar{Q}_{n-1}|^2 + |\bar{D}_n| |\bar{Q}_{n-1}| \sin\left(\Delta\varphi\right)$$
(18)



Fig. 17: MATLAB simulation result of D flip-flop.

$$|Q_m|^2 = \sin^2\left(\frac{\Delta\varphi}{2}\right)|T_0|^2 + \cos^2\left(\frac{\Delta\varphi}{2}\right)|Q_{m-1}|^2 + |T_0| |Q_{m-1}| \sin(\Delta\varphi)$$
(19)

Similarly for  $\bar{Q}_n$  we can write,

$$|\bar{Q}_m|^2 = \sin^2\left(\frac{\Delta\varphi}{2}\right)|\bar{T}_0|^2 + \cos^2\left(\frac{\Delta\varphi}{2}\right)|\bar{Q}_{m-1}|^2 + |\bar{T}_0| |\bar{Q}_{m-1}| \sin\left(\Delta\varphi\right)$$
(20)



Dr. Santosh Kumar

Fig. 18: MATLAB simulation result of T flip-flop.



Dr. Santosh Kumar Fig. 19: Results of the D flip-flop for different combinations of control signals obtained through the BPM.

# Design of Optical Synchronous Counter

Santosh Kumar, et. al., Optical & Quantum Electronics (Springer), Vol. 47, No. 6, (July 26, 2015).

Dr. Santosh Kumar

## Design of Optical Synchronous Counter



Fig. 20: Schematic diagram of a 4-bit synchronous up counter.



Fig. 21: Simulation result of proposed 4-bit synchronous up counter using BPM for different outputs (1000 to 0010)Dr. Santosh Kumar



Fig. 22: Simulation result of proposed 4-bit synchronous up counter using BPM for different outputs (1010 to 0001).
# Design of Programmable Logic Device

Santosh Kumar et. al., Photonic Network communications (Springer), Vol. 33, Issue 3, PP. 356-370 (June 2017).

Dr. Santosh Kumar

## Programmable Logic Device



Figure: (a) Digital circuit of programmable logic device (b) Schematic diagram of using Mach–Zehnder interferometers

## Mathematical Expression for Programmable logic device

$$\begin{aligned} D_{0} &= \cos^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right) \cos^{2}\left(\frac{\Delta \phi_{MZI3}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI7}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI22}}{2}\right) \\ &+ \cos^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI3}}{2}\right) \cos^{2}\left(\frac{\Delta \phi_{MZI6}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI21}}{2}\right) \\ &+ \sin^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right) \cos^{2}\left(\frac{\Delta \phi_{MZI2}}{2}\right) \cos^{2}\left(\frac{\Delta \phi_{MZI5}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI9}}{2}\right) \\ &+ \sin^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI2}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI4}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI10}}{2}\right) \\ O_{1} &= \cos^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI2}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI5}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI10}}{2}\right) \\ &+ \sin^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right) \cos^{2}\left(\frac{\Delta \phi_{MZI2}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI4}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI9}}{2}\right) \\ &+ \sin^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI2}}{2}\right) \cos^{2}\left(\frac{\Delta \phi_{MZI4}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI9}}{2}\right) \\ &+ \sin^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI2}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI4}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI9}}{2}\right) \\ &+ \sin^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI2}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI4}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI9}}{2}\right) \end{aligned}$$
(10)

Dr. Santosh Kumar

#### MATLAB Results for Full Adder



Dr. Santosh Kumar

#### MATLAB Results for Full Subtractor



### MATLAB Results for 2x1 Multiplexer



Figure: MATLAB simulation result of PLD (2x 1 Multiplexer) where A,B,C varies Dr. Santosh Kumar from 000 to 111

## BPM Layout of Programmable Logic device





### Simulation Result from BPM Layout (Full Adder)

Figure: BPM simulation result of PLD (Full adder) where A,B,C varies from 000 to 111 Dr. Santosh Kumar



Simulation Result from BPM Layout (Full Subtractor)

Figure: BPM simulation result of PLD (Full Subtractor) where A,B,C varies from 000 toDr. Santosh Kumar111

### Simulation Result from BPM Layout (2x1 Multiplexer)



## Design of 1 x 4 Signal Router

Santosh Kumar et. al., Optical Engineering (SPIE), vol. 52, no. 03, pp. 035002 (March 04, 2013)

Dr. Santosh Kumar

## 1 x 4 Signal Router



Table 3.3: The output power at the 4 output port on the basis of control signal.

<b>S</b> <sub>1</sub>	$S_2$	<b>S</b> <sub>3</sub>	Output	Output	Output	Output
			port1	port2	port3	port4
6.75V	0 V	'X'	1	0	0	0
6.75V	6.75 V	'X'	0	1	0	0
0 V	'X'	6.75 V	0	0	1	0
0 V	'X'	0 V	0	0	0	1
	1	1	1		1	1









(c)



Figure 3.13: Optical field propagation at various output port depending upon the control signal.

### Mathematical expression of 1x4 Signal Router

The mathematical expression for the normalized output power at the port 1, 2, 3 and 4 as follow;

$$P_{out\,1} = sin^2 \left(\frac{\Delta \varphi_1}{2}\right) cos^2 \left(\frac{\Delta \varphi_2}{2}\right) \quad when \, s_1 = 6.75 V, \, s_2 = 0V \, and \, s_3 = X'$$
 (3.8)

$$P_{out\,2} = \sin^2\left(\frac{\Delta\varphi_1}{2}\right) \cdot \sin^2\left(\frac{\Delta\varphi_2}{2}\right) \quad when \, s_1 = 6.75V, s_2 = 6.75V \text{ and } s_3 = X' \quad (3.9)$$

$$P_{out\,3} = \cos^2\left(\frac{\Delta\varphi_1}{2}\right)\,\sin^2\left(\frac{\Delta\varphi_3}{2}\right) \quad when\,s_1 = 0V, s_2 = \ 'X' \text{ and } s_3 = 6.75V \tag{3.10}$$

$$P_{out 4} = \cos^2\left(\frac{\Delta\varphi_1}{2}\right) \cos^2\left(\frac{\Delta\varphi_3}{2}\right) \quad when \ s_1 = 0V, \ s_2 = \ 'X' \ and \ s_3 = 0V \tag{3.11}$$



### Matlab Output at port 1 and 2



### Matlab Output at port 3 and 4



## Design of 1 x 8 Signal Router

**Santosh Kumar** et. Al., 6<sup>th</sup> IEEE/International Conference on Advanced Infocomm Technology (IEEE/ICAIT-2013), Hsinchu, **Taiwan**, July 2013, IEEE Xplore.

Dr. Santosh Kumar



Figure 3.16: 1 x 8 signal router

### Contd....

Output	$\mathbf{S}_1$	<b>S</b> <sub>2</sub>	<b>S</b> <sub>3</sub>	$S_4$	<b>S</b> <sub>5</sub>	S <sub>6</sub>	$S_7$	<b>S</b> <sub>8</sub>
	(V)	(V)	(V)	(V)	(V)	(V)	(V)	(V)
port1	6.75	0.0	X	0.0	X	X	0.0	Х
port2	6.75	0.0	X	0.0	X	X	6.75	Х
port3	6.75	0.0	X	6.75	X	Х	Х	Х
port4	6.75	6.75	Х	X	6.75	Х	Х	Х
port5	6.75	6.75	Х	Х	0.0	Х	Х	Х
port6	0.0	X	6.75	Х	Х	0.0	Х	Х
port7	0.0	X	6.75	X	X	6.75	Х	6.75
port8	0.0	X	6.75	X	X	6.75	X	0.0

Table 3.3: Different combination of control signal for  $1 \times 8$  Signal router.



Figure 3.17: Optical field propagation at (a) port 1, (b) port 2, (c) port 3, (d) port 4, (e) port 5 (f) port 6, (g) port 7, (h) port 8.

# Design of 4x4 signal router using MZIs

Santosh Kumar et. al., Optics Communication (Elsevier), Vol. 353, PP. 17-26, (May 8, 2015).

Dr. Santosh Kumar

## Design of 4x4 signal router using MZIs



## Mathematical description of 4×4 Signal Router

Depending upon the control signals, the optical power from different input ports can be routed to any one of the four output ports. is calculated as follows;

For output port 1:  

$$0UT1 = \left[\sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right)\cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right)\right]$$
(10)  
For output port 2:  

$$0UT2 = \left[\sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right)\cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right)\cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) \right]$$
(11)  
For output port 3:  

$$0UT3 = \left[\cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) \cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) \right]$$
(12)  
For output port 4:  

$$0UT4 = \left[\sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) \cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) + \sin^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) \cos^{2}\left(\frac{\Delta\phi_{MZI}}{2}\right) \right]$$
(13)



### BPM Results of 4x4 Signal Router



Figure 9: Routing of optical input signal to the four output ports from (a) first input port, (b) second input port, (c) third input port, (d) fourth input port.

# Design of Wavelength Selectors Device

Santosh Kumar et. al., Optics Communications (Elsevier), Vol. 350, PP. 108-118 (April 4, 2015).

Dr. Santosh Kumar



Figure 11: Schematic diagram of  $8 \times 1$  wavelength selector using MZIs

### Mathematical expression of 4x1 Wavelength Selector

The normalized output power for different control signals can be calculated as follows;

$$OUT1 = \left|\frac{OUT1_{MZI3_1}}{E_{in}}\right|^2 = \cos^2\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\cos^2\left(\frac{\Delta\varphi_{MZI2}}{2}\right) \ \cos^2\left(\frac{\Delta\varphi_{MZI3}}{2}\right)$$
(14)

$$OUT2 = \left|\frac{OUT1_{MZI3_2}}{E_{in}}\right|^2 = \cos^2\left(\frac{\Delta\varphi_{MZI1}}{2}\right) \ \cos^2\left(\frac{\Delta\varphi_{MZI2}}{2}\right) \ \sin^2\left(\frac{\Delta\varphi_{MZI3}}{2}\right)$$
(15)

$$OUT3 = \left|\frac{OUT1_{MZI3_3}}{E_{in}}\right|^2 = \sin^2\left(\frac{\Delta\varphi_{MZI1}}{2}\right) \sin^2\left(\frac{\Delta\varphi_{MZI2}}{2}\right) \cos^2\left(\frac{\Delta\varphi_{MZI3}}{2}\right)$$
(16)

$$0UT4 = \left|\frac{0UT1_{MZI3_4}}{E_{in}}\right|^2 = \sin^2\left(\frac{\Delta\varphi_{MZI1}}{2}\right) \sin^2\left(\frac{\Delta\varphi_{MZI2}}{2}\right) \sin^2\left(\frac{\Delta\varphi_{MZI3}}{2}\right)$$
(17)

Dr. Santosh Kumar

### MATLAB Result of 4x1 Wavelength Selector



Figure 12: MATLAB simulation result of  $4 \times 1$  wavelength selector, when  $\lambda_0 - \lambda_3$  is transmitted individually at output port. Dr. Santosh Kumar

## BPM Result of 4x1 Wavelength Selector



Fig.13: Simulation result of (a)  $4 \times 1$  wavelength selector, when (b) only  $\lambda_0$  is transmitted at output port for control signal A = 0 and B = 0



Fig.14: Simulation result of (a)  $4 \times 1$  wavelength selector, when (b) only  $\lambda_1$  is transmitted at output port for control signal A = 0 and B = 1



Fig.15: Simulation result of (a)  $4 \times 1$  wavelength selector, when (b) only  $\lambda_2$  is

transmitted at output port for control signal A = 1 and B = 0

Dr. Santosh Kumar

Control

Signal

A B

1 0

207



Fig.16: Simulation result of (a)  $4 \times 1$  wavelength selector, when (b) only  $\lambda_3$  is transmitted at output port for control signal A = 1 and B = 1

## Mathematical expression of 8x1 Wavelength Selector

The normalized output power for different control signals can be represented by the following equations;

$$0UT1 = \left|\frac{0UT1_{MZI7_1}}{E_{in}}\right|^2 = \cos^2\left(\frac{\Delta\varphi_{MZI4}}{2}\right)\cos^2\left(\frac{\Delta\varphi_{MZI6}}{2}\right)\cos^2\left(\frac{\Delta\varphi_{MZI7}}{2}\right)$$
(18)

$$OUT2 = \left|\frac{OUT1_{MZI7_2}}{E_{in}}\right|^2 = \cos^2\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\cos^2\left(\frac{\Delta\varphi_{MZI5}}{2}\right)\sin^2\left(\frac{\Delta\varphi_{MZI7}}{2}\right)$$
(19)

$$OUT3 = \left|\frac{OUT1_{MZI7_3}}{E_{in}}\right|^2 = \cos^2\left(\frac{\Delta\varphi_{MZI3}}{2}\right) \sin^2\left(\frac{\Delta\varphi_{MZI6}}{2}\right) \cos^2\left(\frac{\Delta\varphi_{MZI7}}{2}\right)$$
(20)

$$0UT4 = \left|\frac{0UT1_{MZI7_4}}{E_{in}}\right|^2 = \cos^2\left(\frac{\Delta\varphi_{MZI2}}{2}\right) \sin^2\left(\frac{\Delta\varphi_{MZI5}}{2}\right) \sin^2\left(\frac{\Delta\varphi_{MZI7}}{2}\right)$$
(21)

$$OUT5 = \left|\frac{OUT1_{MZI75}}{E_{in}}\right|^2 = \sin^2\left(\frac{\Delta\varphi_{MZI4}}{2}\right)\cos^2\left(\frac{\Delta\varphi_{MZI6}}{2}\right) \ \cos^2\left(\frac{\Delta\varphi_{MZI7}}{2}\right)$$
(22)

$$OUT6 = \left|\frac{OUT1_{MZI7_1}}{E_{in}}\right|^2 = \sin^2\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\cos^2\left(\frac{\Delta\varphi_{MZI5}}{2}\right) \sin^2\left(\frac{\Delta\varphi_{MZI7}}{2}\right)$$
(23)

$$OUT7 = \left|\frac{OUT1_{MZI7_3}}{E_{in}}\right|^2 = \sin^2\left(\frac{\Delta\varphi_{MZI3}}{2}\right) \sin^2\left(\frac{\Delta\varphi_{MZI6}}{2}\right) \cos^2\left(\frac{\Delta\varphi_{MZI7}}{2}\right)$$
(24)

$$208 \quad \text{OUT} \Re = \frac{\text{OUT1}_{MZI74}}{E_{in}} \Big|^2 = \sin^2 \left(\frac{\Delta \varphi_{MZI2}}{2}\right) \sin^2 \left(\frac{\Delta \varphi_{MZI5}}{2}\right) \sin^2 \left(\frac{\Delta \varphi_{MZI7}}{2}\right)$$
(25)



### Cont...



Figure 17(b): MATLAB simulation result of  $8 \times 1$  wavelength selector, when  $\lambda_4 - \lambda_7$  is transmitted individually at output port. Dr. Santosh Kumar

## BPM Result of 8x1 Wavelength Selector



Figure 18(a): Simulation results of  $8 \times 1$  wavelength selector, when wavelengths  $(\lambda_0 - \lambda_3)$  are transmitted at output port by applying different control signals

Figure 18(b): Simulation results of  $8 \times 1$  wavelength selector, when wavelengths  $(\lambda_4 - \lambda_7)$  are transmitted at output port by applying different control signals

# Design of Reversible gates

Santosh Kumar et al., Applied optics, Vol. 55. PP.-5693-5701 (OSA) (July, 2016).

Reversible Logic Gates (Feynman gate)



Figure: Logic symbol and Schematic diagram of Feynman gate using MZIs.

### Mathematical Expression for Reversible gates

Mathematical formulation for Feynman gate

$$P = \sin^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right)$$
$$Q = \sin^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right)\cos^{2}\left(\frac{\Delta \phi_{MZI2}}{2}\right) + \cos^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right)\sin^{2}\left(\frac{\Delta \phi_{MZI2}}{2}\right)$$

## MATLAB Results for Feynman gate



Figure: MATLAB simulation result of Feynman gate where A,B varies from 00 to 11 Dr. Santosh Kumar



Figure: BPM layout of Feynman gate
### Simulation Result from BPM (Feynman gate)



Figure: BPM result of Feynman gate where A, B varies from 00 to 11



### Simulation Result (Feynman as D flip flop)



Figure: BPM results of D flip flop

## Reversible Logic Gates (Fredkin)



Figure: Logic symbol and Schematic diagram of Fredkin gate using MZIs.

Mathematical Expression for Reversible gates

Mathematical formulation for Fredkin gate

$$P = \sin^{2}\left(\frac{\Delta \emptyset_{MZI1}}{2}\right)$$
$$Q = \sin^{2}\left(\frac{\Delta \emptyset_{MZI1}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI5}}{2}\right) + \cos^{2}\left(\frac{\Delta \emptyset_{MZI1}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI4}}{2}\right)$$
$$R = \sin^{2}\left(\frac{\Delta \emptyset_{MZI1}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI2}}{2}\right) + \cos^{2}\left(\frac{\Delta \emptyset_{MZI1}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI3}}{2}\right)$$



### MATLAB Results for Fredkin gate



Figure: MATLAB simulation result of Fredkin Gate where A,B,C varies from 000 to 111



Figure: BPM layout of Fredkin gate





Dr. Santosh Kumar

## Simulation Result (Fredkin gate application)

 $Q = \overline{A}$ 

Q = 1

 $Q = \overline{A}$ 

 $\mathbf{Q} = \mathbf{0}$ 

BC

BC

As NOT Gate

A

0 1 0

А

1 1 0



As OR Gate

Figure: BPM result of Fredkin gate used as different applications



# Design of reversible multiplexer

Santosh Kumar et al., Optical Engineering (SPIE) 55(11), 115101 (2016)

Dr. Santosh Kumar

### 2x1 Reversible Multiplexer



Figure: Reversible  $2 \times 1$  multiplexer using MZI.



### Mathematical Expression for 2x1Multiplexer

X,Y,Z is output power calculated for A,B,C respectively.

$$\begin{split} X &= \left[ \sin^2 \left( \frac{\Delta \phi_{MZI1}}{2} \right) \right] \\ Y &= \left[ \sin^2 \left( \frac{\Delta \phi_{MZI2}}{2} \right) \right] \\ Z &= \left[ \sin^2 \left( \frac{\Delta \phi_{MZI1}}{2} \right) \cos^2 \left( \frac{\Delta \phi_{MZI3}}{2} \right) \right] + \left[ \sin^2 \left( \frac{\Delta \phi_{MZI2}}{2} \right) \sin^2 \left( \frac{\Delta \phi_{MZI3}}{2} \right) \right] \end{split}$$



#### MATLAB Results for 2x1 Multiplexer



Figure: MATLAB simulations results of reversible 2x1 multiplexer where C, A, B varies from Dr. Santosh Kumar 000 to 011

### Contd..



Figure: MATLAB simulations results of reversible 2x1 multiplexer where C, A, B varies from Dr. Santosh Kumar 100 to 111



Figure: BPM layout of reversible 2x1 multiplexer

#### Simulation Result from BPM for 2x1 Multiplexer



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Mathematical Expression for 4x1Multiplexer

$$P = \left[\cos^{2}\left(\frac{\Delta\phi_{MZI1}}{2}\right)\cos^{2}\left(\frac{\Delta\phi_{MZI3}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI5}}{2}\right)\right]$$
$$Q = \left[\cos^{2}\left(\frac{\Delta\phi_{MZI1}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI3}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI6}}{2}\right)\right]$$
$$R = \left[\sin^{2}\left(\frac{\Delta\phi_{MZI2}}{2}\right)\cos^{2}\left(\frac{\Delta\phi_{MZI4}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI7}}{2}\right)\right]$$
$$S = \left[\sin^{2}\left(\frac{\Delta\phi_{MZI2}}{2}\right)\sin^{2}\left(\frac{\Delta\phi_{MZI4}}{2}\right)\cos^{2}\left(\frac{\Delta\phi_{MZI8}}{2}\right)\right]$$
$$T = \left[\sin^{2}\left(\frac{\Delta\phi_{MZI1}}{2}\right)\right]$$

$$0 = \left\{ \cos^{2}\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\cos^{2}\left(\frac{\Delta\varphi_{MZI3}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI5}}{2}\right) \right\} + \left\{ \cos^{2}\left(\frac{\Delta\varphi_{MZI1}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI3}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI6}}{2}\right) \right\} + \left\{ \sin^{2}\left(\frac{\Delta\varphi_{MZI2}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI4}}{2}\right)\cos^{2}\left(\frac{\Delta\varphi_{MZI4}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI7}}{2}\right) \right\} + \left\{ \sin^{2}\left(\frac{\Delta\varphi_{MZI2}}{2}\right)\sin^{2}\left(\frac{\Delta\varphi_{MZI4}}{2}\right)\cos^{2}\left(\frac{\Delta\varphi_{MZI8}}{2}\right) \right\}$$

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Figure: MATLAB simulations results of reversible 4x1 multiplexer where varies from 00 Dr. Santosh Kumar to 11

### BPM Layout of 4x1Multiplexer



Figure: BPM layout of reversible 2x1 multiplexer



### Simulation Result from BPM for 4x1 Multiplexer



Figure: BPM results for 4x1 Multiplexer

# Design of Reversible Sequential Circuits

Santosh Kumar et. al., Optical Engineering (SPIE) 55(12),125105 (2016).



Dr. Santosh Kumar

## Logic Diagram of different sequential circuits



Figure: (a) D Flip-flop using Fredkin gate (b) T Flip-flop using Peres gate



Figure: S-R Flip-flop using Feynman and Peres gate (a) block level design (b) gate level design



Figure: J-K Flip-flop using Feynman and Fredkin gate (a) block level design (b) gate level design Dr. Santosh Kumar

# D Flip-flop



Figure: D Flip-flop using Feynman

### Mathematical Expression for D flip-flop

Mathematical formulation for D flip-flop can be calculated as:

$$Z = \sin^{2}\left(\frac{\Delta \emptyset_{MZI1}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI2}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI6}}{2}\right) + \cos^{2}\left(\frac{\Delta \emptyset_{MZI1}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI3}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI6}}{2}\right)$$

### MATLAB Results for D flip-flop



to 111



# T Flip-flop



Figure: T Flip-flop using Peres gate

## Mathematical Expression for T flip-flop

Mathematical formulation for T flip-flop can be calculated as:

$$Z = \sin^{2}\left(\frac{\Delta \emptyset_{MZI3}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI4}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI5}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI8}}{2}\right) + \sin^{2}\left(\frac{\Delta \emptyset_{MZI3}}{2}\right) \cos^{2}\left(\frac{\Delta \emptyset_{MZI4}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI5}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI8}}{2}\right) + \cos^{2}\left(\frac{\Delta \emptyset_{MZI3}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI7}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI8}}{2}\right)$$

## MATLAB Results for T flip-flop



Figure: MATLAB simulation results of D flip-flop using Fredkin gate where input signal E, D, Q varies from 100 to Dr. Santosh Kumar 111



S-R Flip-flop



Figure: S-R flip-flop using Peres gate and Feynman gate

#### Mathematical Expression for S-R code converter

Mathematical formulation for S-R flip-flop can be calculated as:

$$D = \sin^{2}\left(\frac{\Delta \emptyset_{MZI5}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI6}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI7}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI10}}{2}\right) + \sin^{2}\left(\frac{\Delta \emptyset_{MZI5}}{2}\right) \cos^{2}\left(\frac{\Delta \emptyset_{MZI6}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI8}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI10}}{2}\right) + \cos^{2}\left(\frac{\Delta \emptyset_{MZI5}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI9}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI10}}{2}\right)$$

### MATLAB Results for S-R flip-flop



Figure: MATLAB simulation results of S-R flip-flop using Feynman gate and Peres gate where input signal S, R, Q varies from 000 to 011

Dr. Santosh Kumar

## Contd..



Figure: MATLAB simulation results of S-R flip-flop using Feynman gate and Peres gate where input signal S, R, Q Dr. Santosh Kumar varies from 100 to 111


Figure: BPM layout of S-R Flip-flop using Feynman and Peres gate



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Figure: BPM simulation results for S-R flip-flop



## Mathematical Expression for J-K flip flop

Mathematical formulation for J-K flip-flop can be calculated as:

$$D = \sin^{2}\left(\frac{\Delta \emptyset_{MZI8}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI9}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI9}}{2}\right) \\ + \cos^{2}\left(\frac{\Delta \emptyset_{MZI8}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI9}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI10}}{2}\right)$$

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MATLAB Results for J-K flip-flop



Figure: MATLAB simulation results of J-K flip-flop using Feynman gate and Fredkin gate where input signal Q, J, K varies from 000 to 011

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Contd..

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Figure: MATLAB simulation results of J-K flip-flop using Feynman gate and Fredkin gate where input Dr. Santosh Kumar signal Q, J, K varies from 100 to 111



# Design of Optical Reversible gate (Peres Gate)

Santosh Kumar et. al., OSA Fio2016, Rochester, New York, USA. (Oct 17-21,2016)



Dr. Santosh Kumar



## MATLAB Results for Reversible gate



Figure: MATLAB Simulation result of proposed Peres gate where input A, B, C varies from 000 to



Figure: BPM result of proposed Peres gate where input A, B, C varies from 000 to 111 Dr. Santosh Kumar



# Ultrafast Optical Reversible Double Feynman logic gate

Santosh Kumar et al., Proc. SPIE 10105, Oxide-based Materials and Devices VIII, SPIE Photonics West - 2017, San Francisco, California, USA, PP. 1010520 (28 Jan. - 2 Feb. 2017).





Truth table and mathematical expression for double Feynman gate

$$P = \sin^2\left(\frac{\Delta \phi_{MZI3}}{2}\right)$$

$$Q = \sin^{2}\left(\frac{\Delta \phi_{MZI3}}{2}\right) \cos^{2}\left(\frac{\Delta \phi_{MZI4}}{2}\right) + \cos^{2}\left(\frac{\Delta \phi_{MZI3}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI4}}{2}\right)$$
$$R = \sin^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right) \cos^{2}\left(\frac{\Delta \phi_{MZI2}}{2}\right) + \cos^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI2}}{2}\right)$$

Input			outp	output		
Α	B	С	Р	Q	R	
0	0	0	0	0	0	
0	0	1	0	0	1	
0	1	0	0	1	0	
0	1	1	0	1	1	
1	0	0	1	1	1	
1	0	1	1	1	0	
1	1	0	1	0	1	
1	1	1	1	0	0	

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### MATLAB simulation results



Figure: MATLAB simulation results where input signal A; B and C varies from 000 Dr. Santosh Kumar to 011 Contd..



Figure: MATLAB simulation results where input signal A; B and C varies from 100 to

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#### **BPM** simulation results



# Design of Peres gate and its applications

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### Peres gate and its applications



(b)

(c)

Figure: Logic design of Peres gate and its application as full-adder and T flip-flop



Figure: Schematic of Peres gate using Mach-Zehnder interferometer

Mathematical expression for Peres gate

$$P = \sin^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right)$$

$$Q = \sin^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right)\cos^{2}\left(\frac{\Delta \phi_{MZI2}}{2}\right) + \cos^{2}\left(\frac{\Delta \phi_{MZI1}}{2}\right)\sin^{2}\left(\frac{\Delta \phi_{MZI2}}{2}\right)$$

$$R = \sin^{2}\left(\frac{\Delta \phi_{MZI3}}{2}\right)\sin^{2}\left(\frac{\Delta \phi_{MZI4}}{2}\right)\cos^{2}\left(\frac{\Delta \phi_{MZI5}}{2}\right)$$

$$+ \sin^{2}\left(\frac{\Delta \phi_{MZI3}}{2}\right)\cos^{2}\left(\frac{\Delta \phi_{MZI4}}{2}\right)\sin^{2}\left(\frac{\Delta \phi_{MZI6}}{2}\right)$$

$$+ \cos^{2}\left(\frac{\Delta \phi_{MZI3}}{2}\right)\sin^{2}\left(\frac{\Delta \phi_{MZI7}}{2}\right)$$

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Figure: MATLAB simulation results of Peres gate where A, B, C varies from 000 to 011

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### MATLAB Simulation Results



Figure: MATLAB simulation results of Peres gate where A, B, C varies from 100 to 111 Dr. Santosh Kumar

## Full Adder using Peres gate



Figure: Schematic of full-adder using MZI based Peres gate

# Mathematical expression for Full adder using Peres gate

$$Q = \sin^2\left(\frac{\Delta \phi_{MZI1}}{2}\right) \cos^2\left(\frac{\Delta \phi_{MZI2}}{2}\right) + \cos^2\left(\frac{\Delta \phi_{MZI1}}{2}\right) \sin^2\left(\frac{\Delta \phi_{MZI2}}{2}\right)$$

$$R = \sin^{2}\left(\frac{\Delta \phi_{MZI3}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI4}}{2}\right) \cos^{2}\left(\frac{\Delta \phi_{MZI5}}{2}\right) + \sin^{2}\left(\frac{\Delta \phi_{MZI3}}{2}\right) \cos^{2}\left(\frac{\Delta \phi_{MZI4}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI6}}{2}\right) + \cos^{2}\left(\frac{\Delta \phi_{MZI3}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI7}}{2}\right)$$

Sum = 
$$\sin^2\left(\frac{\Delta\phi_{MZI8}}{2}\right)\cos^2\left(\frac{\Delta\phi_{MZI9}}{2}\right) + \cos^2\left(\frac{\Delta\phi_{MZI8}}{2}\right)\sin^2\left(\frac{\Delta\phi_{MZI9}}{2}\right)$$

$$Carry = \sin^{2}\left(\frac{\Delta \phi_{MZI10}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI11}}{2}\right) \cos^{2}\left(\frac{\Delta \phi_{MZI12}}{2}\right) + \sin^{2}\left(\frac{\Delta \phi_{MZI10}}{2}\right) \cos^{2}\left(\frac{\Delta \phi_{MZI11}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI13}}{2}\right) + \cos^{2}\left(\frac{\Delta \phi_{MZI10}}{2}\right) \sin^{2}\left(\frac{\Delta \phi_{MZI14}}{2}\right)$$

#### MATLAB Simulation Results of Full adder



Figure: MATLAB simulation results of full-adder using Peres gate where A, B, C varies from 000



Figure: MATLAB simulation results of full-adder using Peres gate where A, B, C varies from 100

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to 111

# T Flip-flop using Peres gate and its mathematical expression



Figure: Schematic of T Flip-flop using Peres gate

$$Z = \sin^{2}\left(\frac{\Delta \emptyset_{MZI3}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI4}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI5}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI8}}{2}\right) + \sin^{2}\left(\frac{\Delta \emptyset_{MZI3}}{2}\right) \cos^{2}\left(\frac{\Delta \emptyset_{MZI4}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI6}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI8}}{2}\right) + \cos^{2}\left(\frac{\Delta \emptyset_{MZI3}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI7}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI8}}{2}\right)$$

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## MATLAB Simulation Results of T-Flip flop



Figure: MATLAB simulation results of T- flip-flop using Peres gate where input signal E, T, Q varies from 100 to 111



Figure: BPM simulation result of reversible Peres gate using MZI

## BPM layout of Full adder using Peres gate



Figure: BPM layout of reversible Full adder using MZI based Peres gate.

### Simulation Result of Full adder





Figure: BPM layout of reversible T- flip-flop using MZI based Peres gate



Figure: BPM simulation result of reversible T- flip-flop using MZI based Peres gate



# Design of Reversible Full adder using Peres gate

- ≻ Figure 10 shows the logic diagram of full adder using Peres gate.
- As shown in Fig.10 (a), Peres gate is having 3 outputs which equals to  $P = A, Q = A \oplus B$  and  $R = (A, B) \oplus C$  respectively.
- ➤ In Fig. 10 (b), it is shown that by using two Peres gate in cascading, one can design reversible full-adder circuit.
- > The third input of first Peres gate is ancilla input  $C_{in}$ , which is equals to 0 and first output is garbage output.
- By cascading second and third output of first gate as inputs to second Peres gate, sum and carry output of full adder circuit will be available at second and third output port of second Peres gate respectively.



Figure 10: Logic design of reversible full-adder using Peres gate Dr. Santosh Kumar

## cont...

≻ Figure 11 shows the equivalent MZI diagram of the circuit.

Photo detector and amplifier is used to convert optical signal to electrical form to control the electrode voltage.



Dr. Santosh Kumar Figure 11: Schematic of full-adder using MZI based Peres gate



Figure: Layout diagram of Reversible Full Adder using MZIs

### **MATLAB Simulation results**



Figure: MATLAB simulation results where input(A,B,C) varies from 000 to 011

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# Optical reversible hybrid Adder/Subtractor

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## MZI diagram of Reversible Adder/Subtractor



Dr. Santosh Kumar Figure: MZI diagram of Full adder subtractor

## Mathematical expression for reversible addersubtractor

Sum/Difference = 
$$\sin^2\left(\frac{\Delta \emptyset_{MZI10}}{2}\right)\cos^2\left(\frac{\Delta \emptyset_{MZI11}}{2}\right)$$
  
+  $\cos^2\left(\frac{\Delta \emptyset_{MZI10}}{2}\right)\sin^2\left(\frac{\Delta \emptyset_{MZI11}}{2}\right)$ 

Carry/Borrow

$$= \sin^{2}\left(\frac{\Delta \emptyset_{MZI12}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI13}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI14}}{2}\right) \\ + \sin^{2}\left(\frac{\Delta \emptyset_{MZI12}}{2}\right) \cos^{2}\left(\frac{\Delta \emptyset_{MZI13}}{2}\right) \cos^{2}\left(\frac{\Delta \emptyset_{MZI15}}{2}\right) \\ + \cos^{2}\left(\frac{\Delta \emptyset_{MZI12}}{2}\right) \sin^{2}\left(\frac{\Delta \emptyset_{MZI15}}{2}\right)$$

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Figure: MATLAB simulation results of proposed device as Full adder where A, B, CDr. Santosh Kumarvaries from 000 to 011

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Figure: MATLAB simulation results of proposed device as Full adder where A, B, CDr. Santosh Kumarvaries from 100 to 111.

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Figure: MATLAB simulation results of proposed device as Full subtractor where A, B,Dr. Santosh KumarC varies from 000 to 011.

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Figure: MATLAB simulation results of proposed device as Full subtractor where A, B,Dr. Santosh KumarC varies from 100 to 111



Figure: BPM layout of Hybrid Full adder/subtractor using TR gate

#### **BPM Simulation Result**

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Figure: Optical field pattern of proposed device as full adder using BPM while inputDr. Santosh Kumarsignal A, B, C varies from 000 to 111

### **BPM Simulation Result**



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inputs signal A, B, C varies from 000 to 111

# Design of Reversible TR gate

Santosh Kumar et al, OSA FiO-2017, Washington D.C, USA. (Sept 16-22, 2017)



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Figure: Schematic diagram of TR gate using lithium niobate based MZI





Figure: MATLAB simulation results where A, B, C varies from 000 to 011.

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Figure: BPM simulation results where Inputs A, B, C varies from 000 to 111. Dr. Santosh Kumar

# Study and analysis of some factors influencing the performances of proposed devices

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# Performance parameters

- The factors which influences the performance of the devices are
- transmission loss
- $\succ$  cross talk
- $\succ$  extinction ratio
- variation of bit rate



## Variation of transition loss



Figure: Variation of loss with respect to Ti- thickness  $(t_s)$  for (a) straight waveguide and (b) curved (S-bend) waveguide for operating wavelength 1.3  $\mu$ m.

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## Crosstalk



Figure: Representation of crosstalk level with variation of power imbalance (Switch state : Cross) for operating wavelength 1.3 μm.

#### Cont.....



Figure: Calculated cross-talk levels due to variation in Ti-thickness for operating wavelength  $1.3 \mu m$ ; (switch state: Cross).

### Variation of extinction ratio



Figure: Extinction ratio for an modulator versus the optical power difference between its two arms

## Variation of bit rate



Figure: Variation of bit rate with respect to length of MZI.

## Variation of chromatic dispersion and modal dispersion

The chromatic dispersion of a single  $LiNbO_3$  based MZI is given by (Raghavendra and Prasad 2010);

$$D_c = -\left(\frac{L_m \cdot \Delta \lambda \cdot \lambda}{c}\right) \cdot \left(\frac{d^2 n_e}{d\lambda^2}\right)$$

Where

 $L_m \rightarrow$  the length of a single MZI.

 $\lambda \rightarrow$  the operating wavelength.

 $\Delta\lambda \rightarrow$  the spectral line width of optical source.

 $n_e \rightarrow$  the effective refractive index of the material (LiNbO<sub>3</sub>).

The modal dispersion,  $D_{modal}\;$  for a multimode step-index electro-optic device with length  $L_m$  is given by

$$D_m = \frac{L_m n_e \Delta n_e}{c}$$

 $\Delta n_e$  is the relative refractive index difference.

The total dispersion coefficient  $\boldsymbol{D}_{total}\,$  is given by

 $D_{total} = D_m + D_c$ 



Figure: Variation of chromatic dispersion with respect to length of

MZI.



Figure: Variation of modal dispersion with increase in length of MZI.



#### Future scope

- In this study, a thorough study of LiNbO<sub>3</sub> based MZIs is performed to design various optical signal processing devices. However, more compact devices having less complexity may be proposed further to get better performance.
- By using the applied electrode voltage and some of the sensing material in one arm of MZI, it can be used for designing the ultra-efficient optical modulator and sensors.
- On the basis of the simulation results; a 3-dB coupler, Mach-Zehnder interferometer and other optical integrated devices can be fabricated.

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# THANKYOU

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